

Neural Architecture Search

EECE695D: Efficient ML Systems

Spring 2025

Recap

- Suppose that we have:
 - a neural network architecture, denoted by **arch**
 - an optimization algorithm, denoted by **opt**

- **KD.** Given a small NN architecture, optimize it well?

$$\min_{\text{opt}} \text{loss}(\text{arch}, \text{opt})$$

($\text{loss}(\cdot, \cdot)$ denotes the loss after training)

Overview

- Consider optimizing another variable:
 - Find a NN architecture that can be trained well

$$\min_{\text{arch}} \text{loss}(\text{arch}, \text{opt})$$

- Put a constraint / regularizer on the $\text{size}(\text{arch})$
 - FLOPs
 - Memory constraint

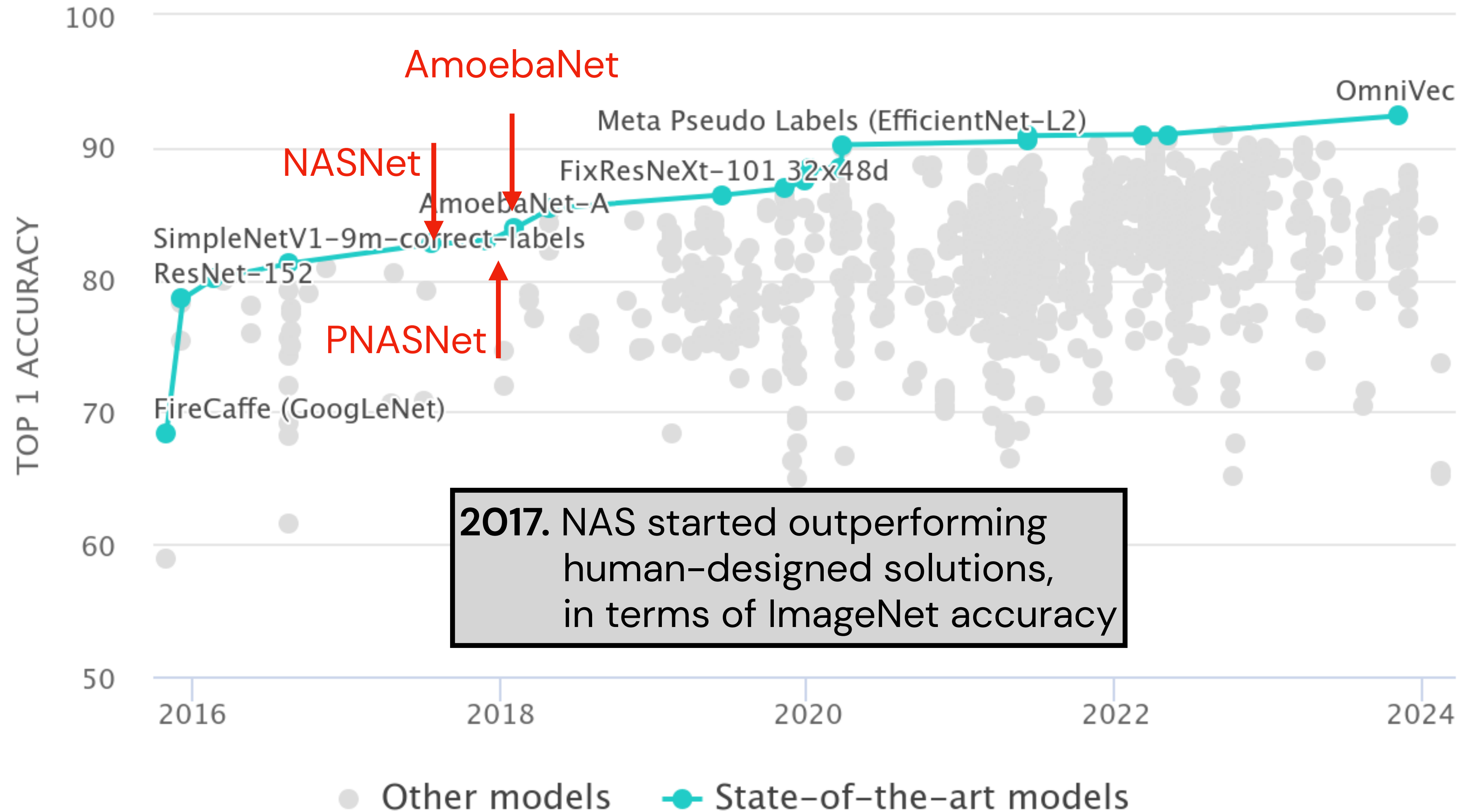
Motivation

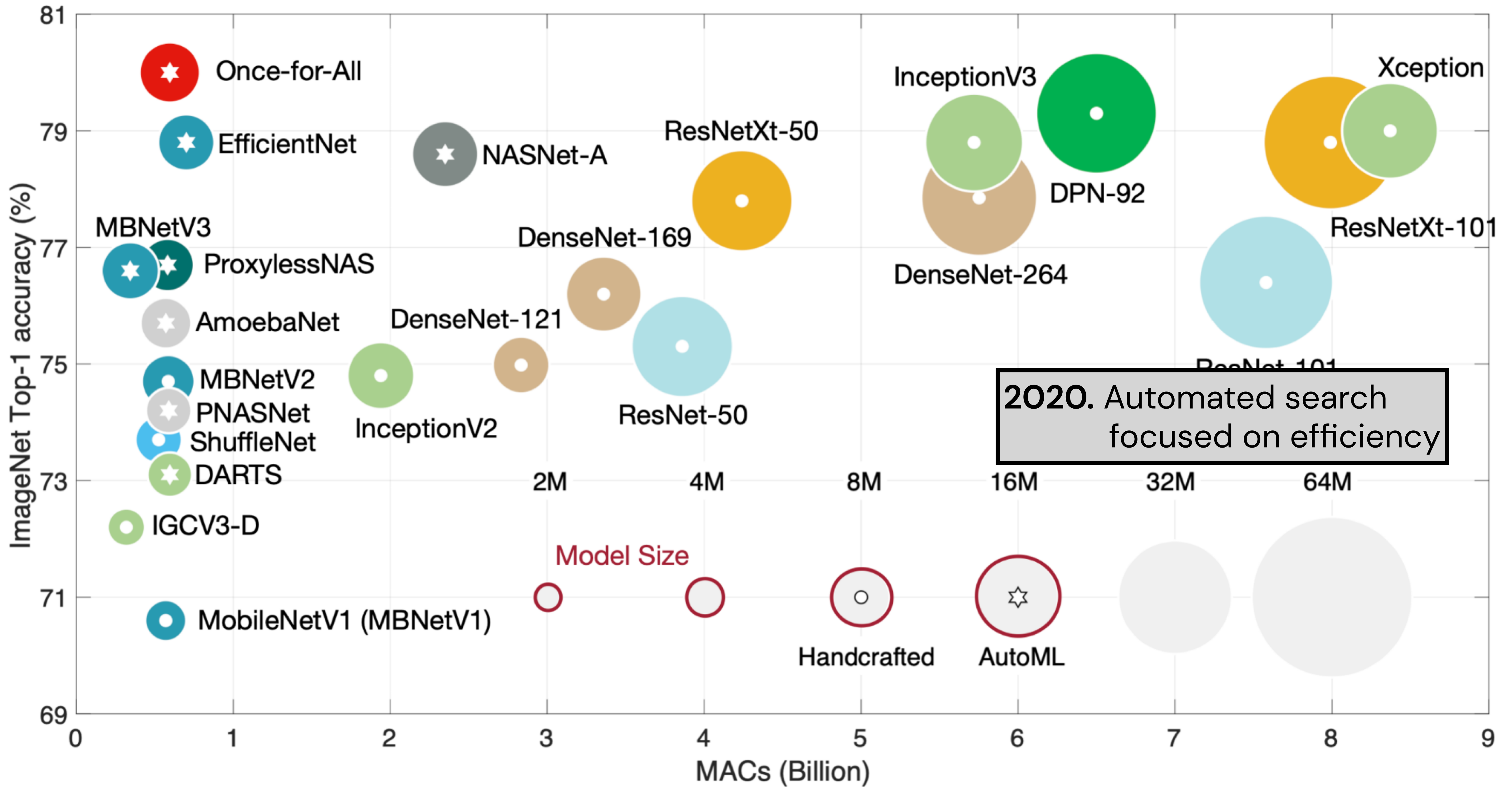
- **Old solution.** Let 🧑 optimize
 - Number of layers
 - Number of channels (in each layer)
 - Activation function
 - Operator type
 - (...)
- **NAS.** Let 🤖 optimize!

Input	Operator	exp size	#out	SE	NL	<i>s</i>
$224^2 \times 3$	conv2d	-	16	-	HS	2
$112^2 \times 16$	bneck, 3x3	16	16	-	RE	1
$112^2 \times 16$	bneck, 3x3	64	24	-	RE	2
$56^2 \times 24$	bneck, 3x3	72	24	-	RE	1
$56^2 \times 24$	bneck, 5x5	72	40	✓	RE	2
$28^2 \times 40$	bneck, 5x5	120	40	✓	RE	1
$28^2 \times 40$	bneck, 5x5	120	40	✓	RE	1
$28^2 \times 40$	bneck, 3x3	240	80	-	HS	2
$14^2 \times 80$	bneck, 3x3	200	80	-	HS	1
$14^2 \times 80$	bneck, 3x3	184	80	-	HS	1
$14^2 \times 80$	bneck, 3x3	184	80	-	HS	1
$14^2 \times 80$	bneck, 3x3	480	112	✓	HS	1
$14^2 \times 112$	bneck, 3x3	672	112	✓	HS	1
$14^2 \times 112$	bneck, 5x5	672	160	✓	HS	2
$7^2 \times 160$	bneck, 5x5	960	160	✓	HS	1
$7^2 \times 160$	bneck, 5x5	960	160	✓	HS	1
$7^2 \times 160$	conv2d, 1x1	-	960	-	HS	1
$7^2 \times 960$	pool, 7x7	-	-	-	-	1
$1^2 \times 960$	conv2d 1x1, NBN	-	1280	-	HS	1
$1^2 \times 1280$	conv2d 1x1, NBN	-	k	-	-	1

Table 1. Specification for MobileNetV3-Large. SE denotes whether there is a Squeeze-And-Excite in that block. NL denotes the type of nonlinearity used. Here, HS denotes h-swish and RE denotes ReLU. NBN denotes no batch normalization. *s* denotes stride.

Motivation





Basic idea

Idea

- Ultimately, NAS is about solving

$$\min_{a \in \mathcal{A}} \ell(a)$$

- \mathcal{A} : Search space (e.g., all possible neural nets)
- $\ell(\cdot)$: Test loss after training
- **Problem.**
 - Search space is too big
 - Search space is discrete
 - Evaluating loss $\ell(\cdot)$ takes much compute

Idea

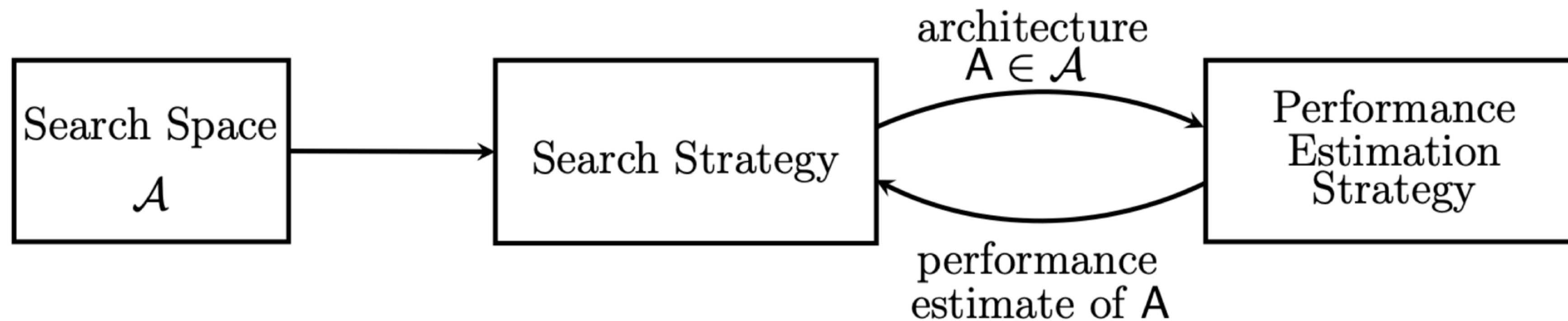
$$\min_{a \in \mathcal{A}} \ell(a)$$

- **Dumb Approach.** A computational nightmare
 - Construct \mathcal{A} as a set of all possible neural nets
 - Pick a model $a \in \mathcal{A}$
 - Train it until convergence
 - Evaluate $\ell(a)$
 - Repeat, until we evaluate all models

Elements

$$\min_{a \in \mathcal{A}} \ell(a)$$

- **Trick.** Simplify the problem in three senses:
 - Search space. Use human / experience-based priors
 - Search strategy. Discrete search algorithms or relaxation
 - Evaluation strategy. Use cheaper proxies



Search space

Search space

$$\min_{a \in \mathcal{A}} \ell(a)$$

- Defines which architecture can be represented
- **Idea.** Narrow down with human priors
- Look at many different levels:
 - Elementary Ops
 - Blocks
 - Cells

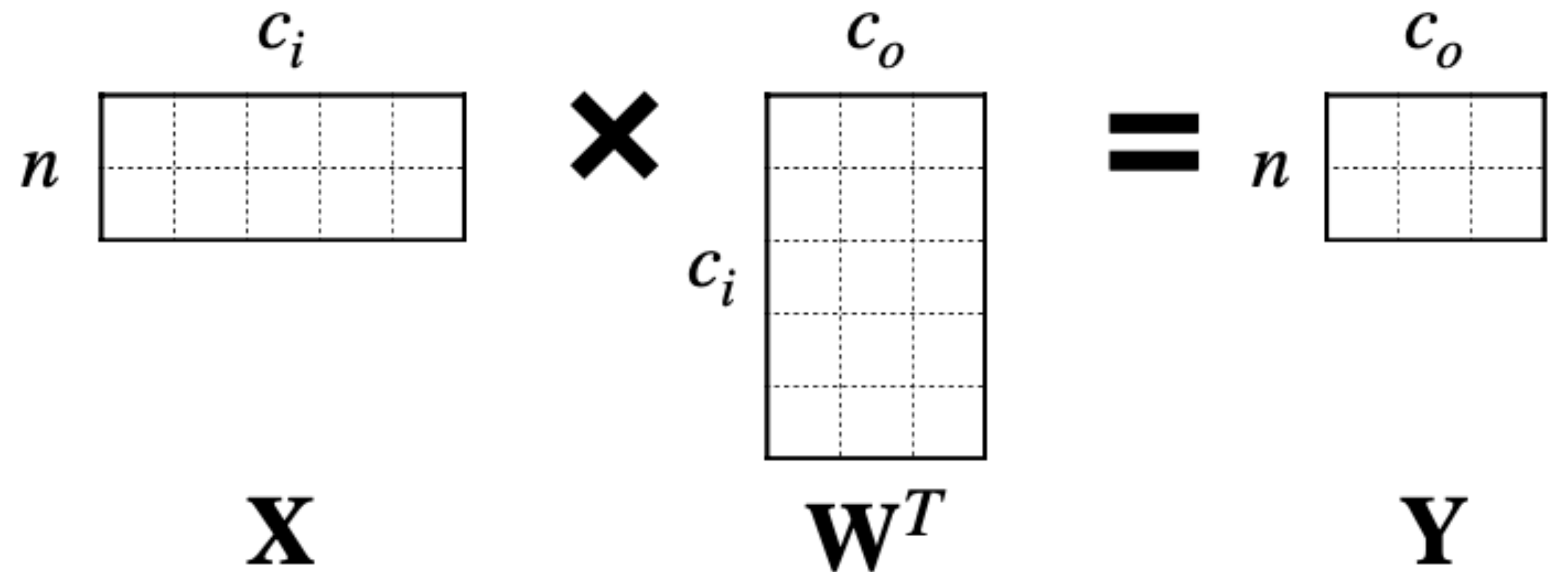
Elementary Ops

- Already much effort to improve the efficiency
 - Recap

Linear

- a.k.a. Dense layer / Fully-connected layer
 - Matrix multiplication

- **Params.** $C_i \cdot C_o$
- **Compute.** $C_i \cdot C_o$

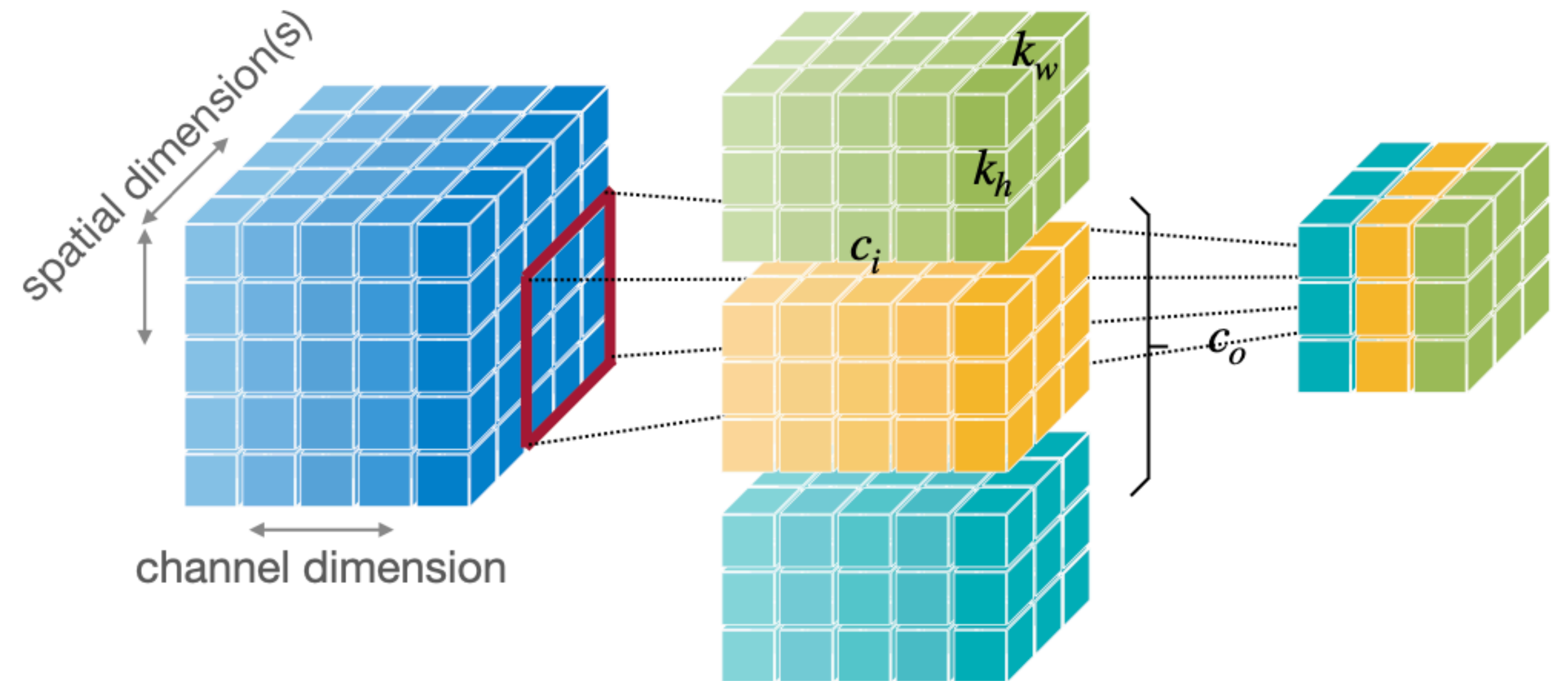


Convolution

- Parameter sharing for efficiency

- **Params.** $k_h k_w c_i c_o$
(reduced by $h_i w_i h_o w_o / k_h k_w$)

- **Compute.** $k_h k_w c_i c_o h_o w_o$
(reduced by $h_i w_i / k_i k_o$)



Grouped convolution

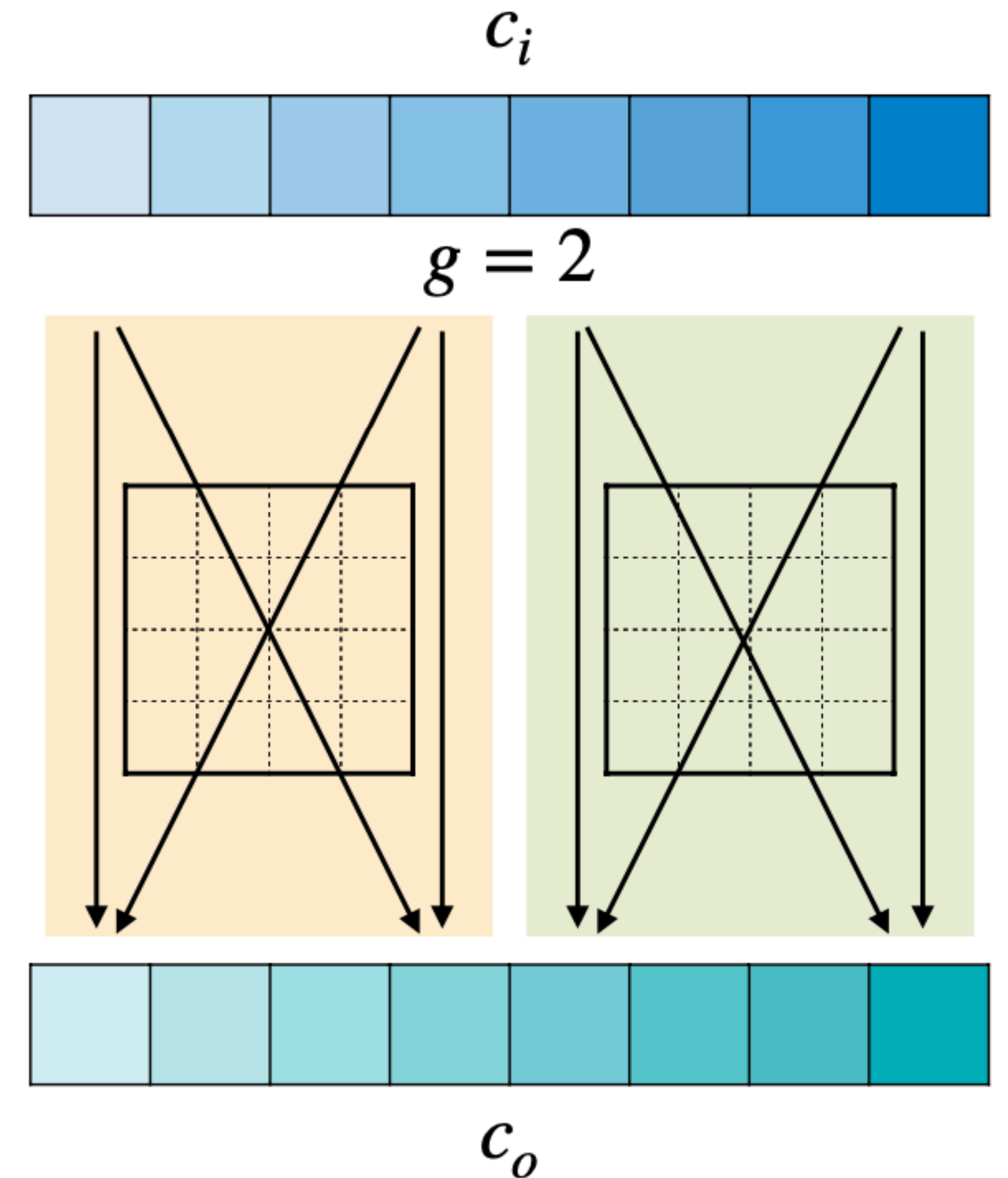
- Certain input channels only affect certain output channels

- **Params.** $k_h k_w c_i c_o / g$

(reduced by g)

- **Compute.** $k_h k_w c_i c_o h_o w_o / g$

(reduced by g)



Depthwise convolution

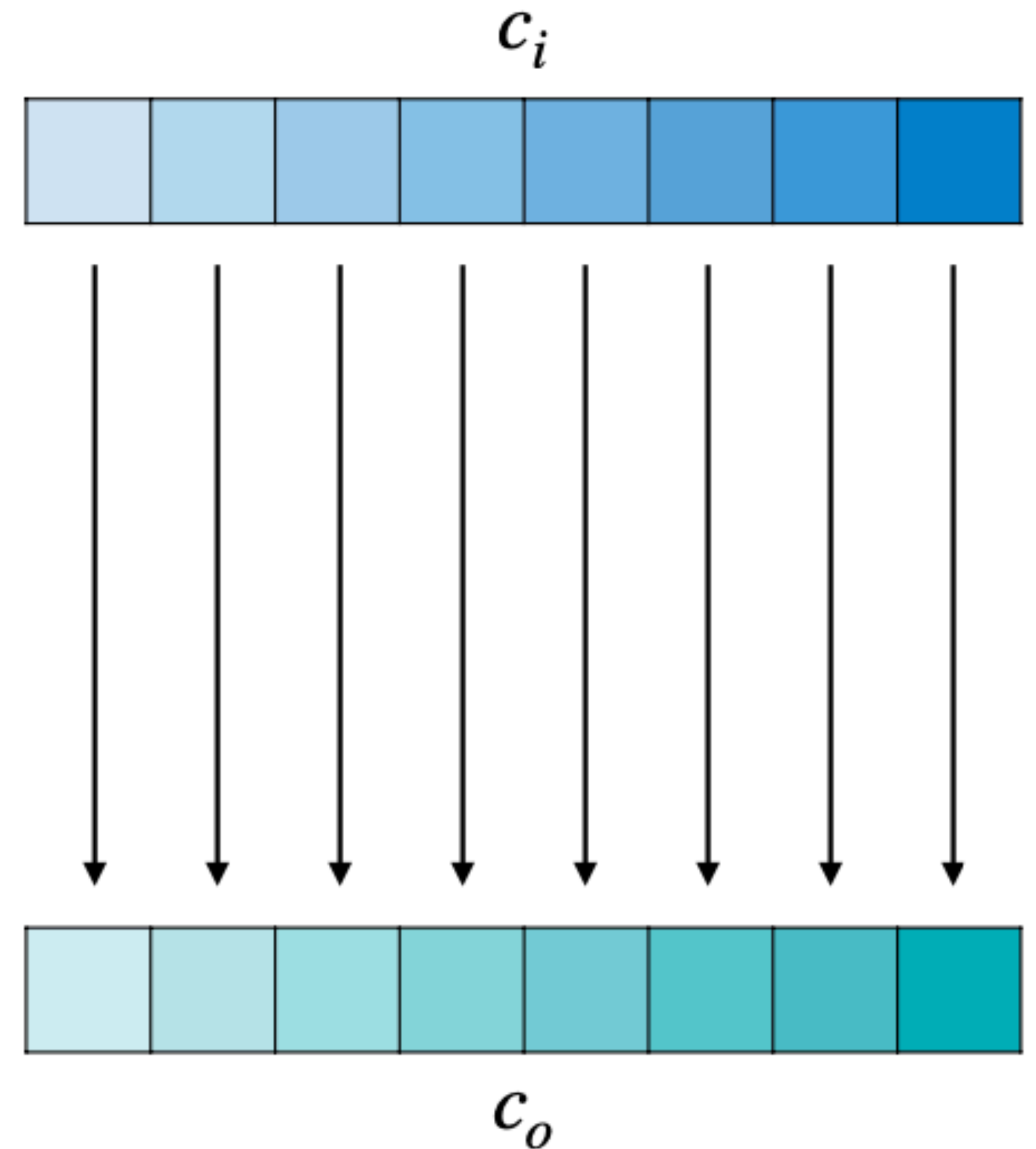
- Group for every channel
 - Linear increase in cost in terms of the #channels (\Leftrightarrow quadratic)

- **Params.** $k_h k_w c$

(reduced by c over conv2d)

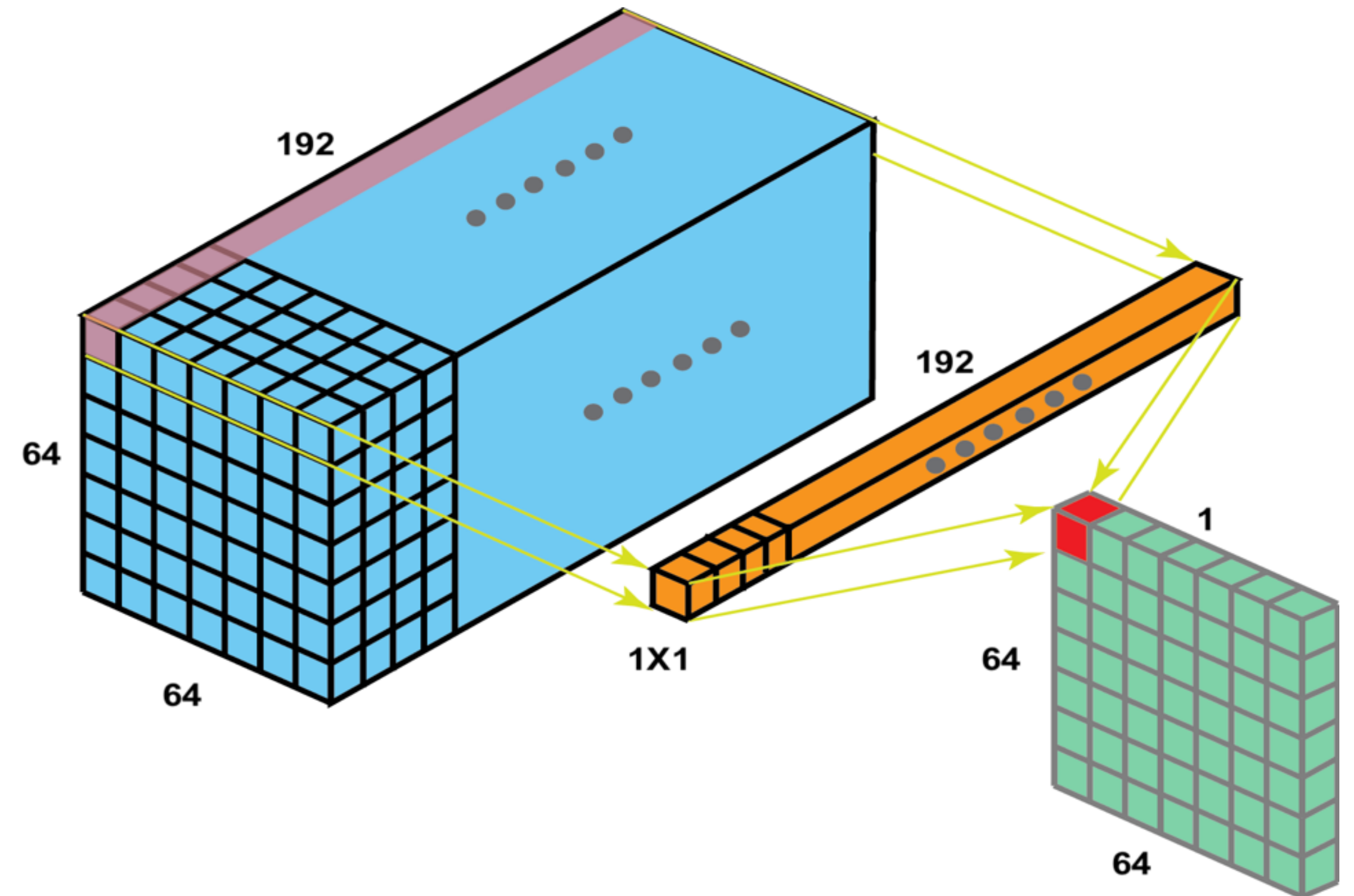
- **Compute.** $k_h k_w h_o w_o c$

(reduced by c over conv2d)



1x1 convolution

- Only mixes information between channels
 - Complementary to depthwise
- Params. c^2
- Compute. $h_i w_i c^2$



Handmade blocks

- Many works have already combined several ops into **blocks**
 - Focused on efficiency
 - Will be a motivation of how we build search space

MobileNet: Depthwise + 1x1

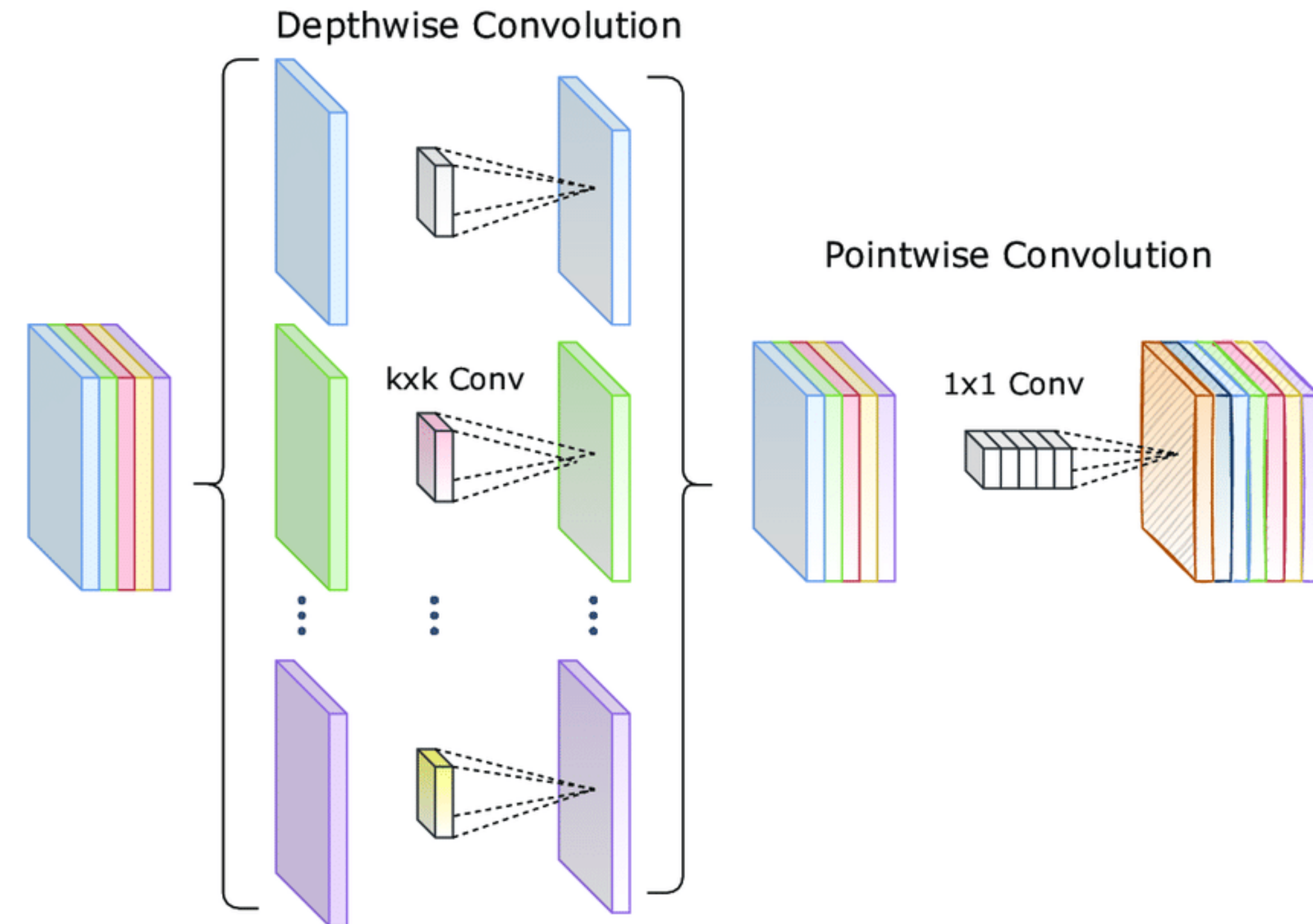
- Depthwise Conv → 1x1 Conv
(intra-channel) (inter-channel)

- c.f. transformers

- By replacing Conv → Depthwise + 1x1:

- **Params.** $k^2c^2 \rightarrow k^2c + c^2$

- **Compute.** $hwk^2c^2 \rightarrow hw(k^2c + c^2)$

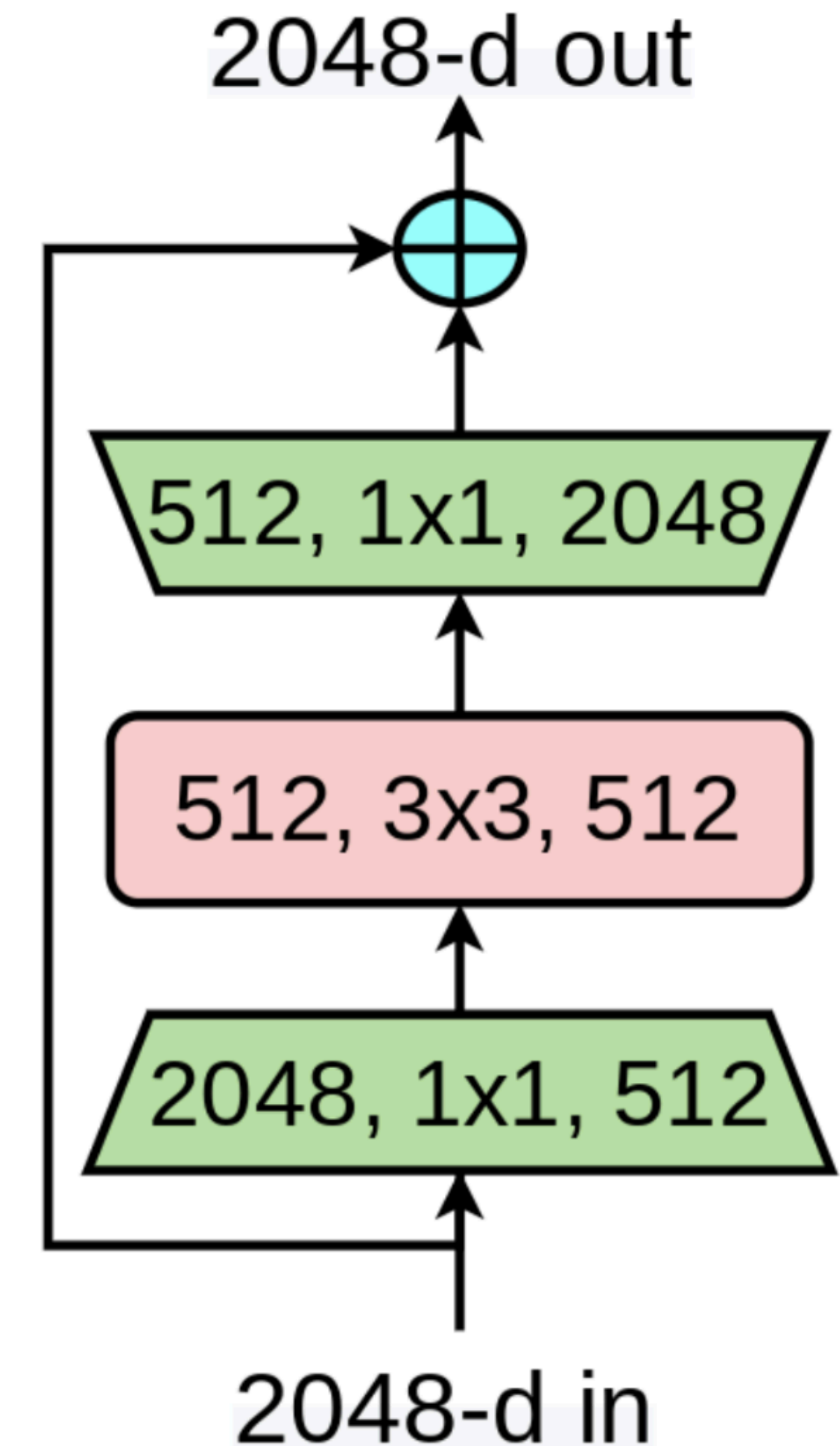


ResNet: Bottlenecks

- Decrease #channels \rightarrow do 3x3 \rightarrow increase back
- By replacing Conv \rightarrow Bottleneck:
(with channel reduction factor r)

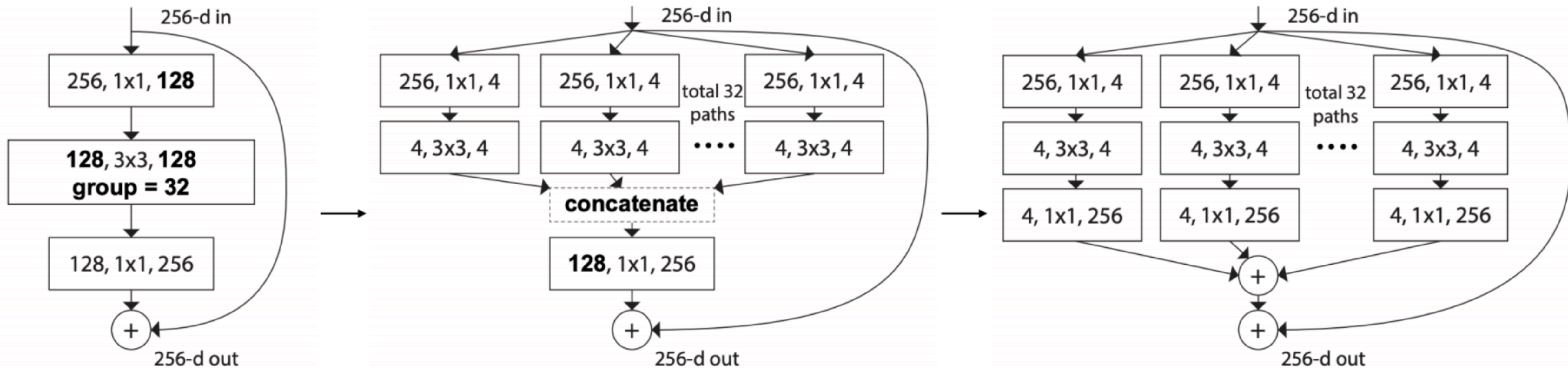
- **Params.** $k^2c^2 \rightarrow (2/r + k^2/r^2)c^2$

- **Compute.** $hwk^2c^2 \rightarrow hw(2c^2/r + k^2c^2/r^2)$



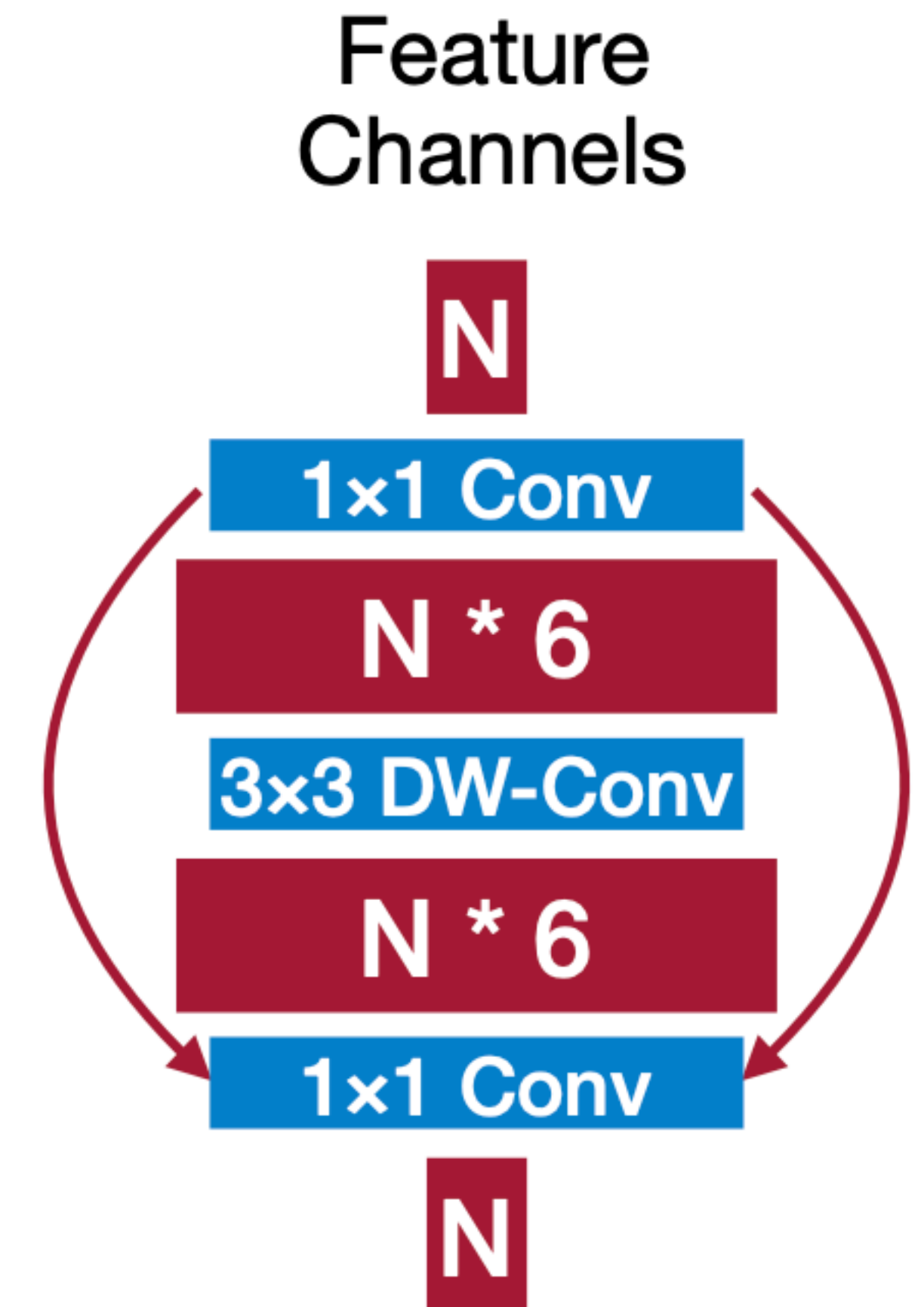
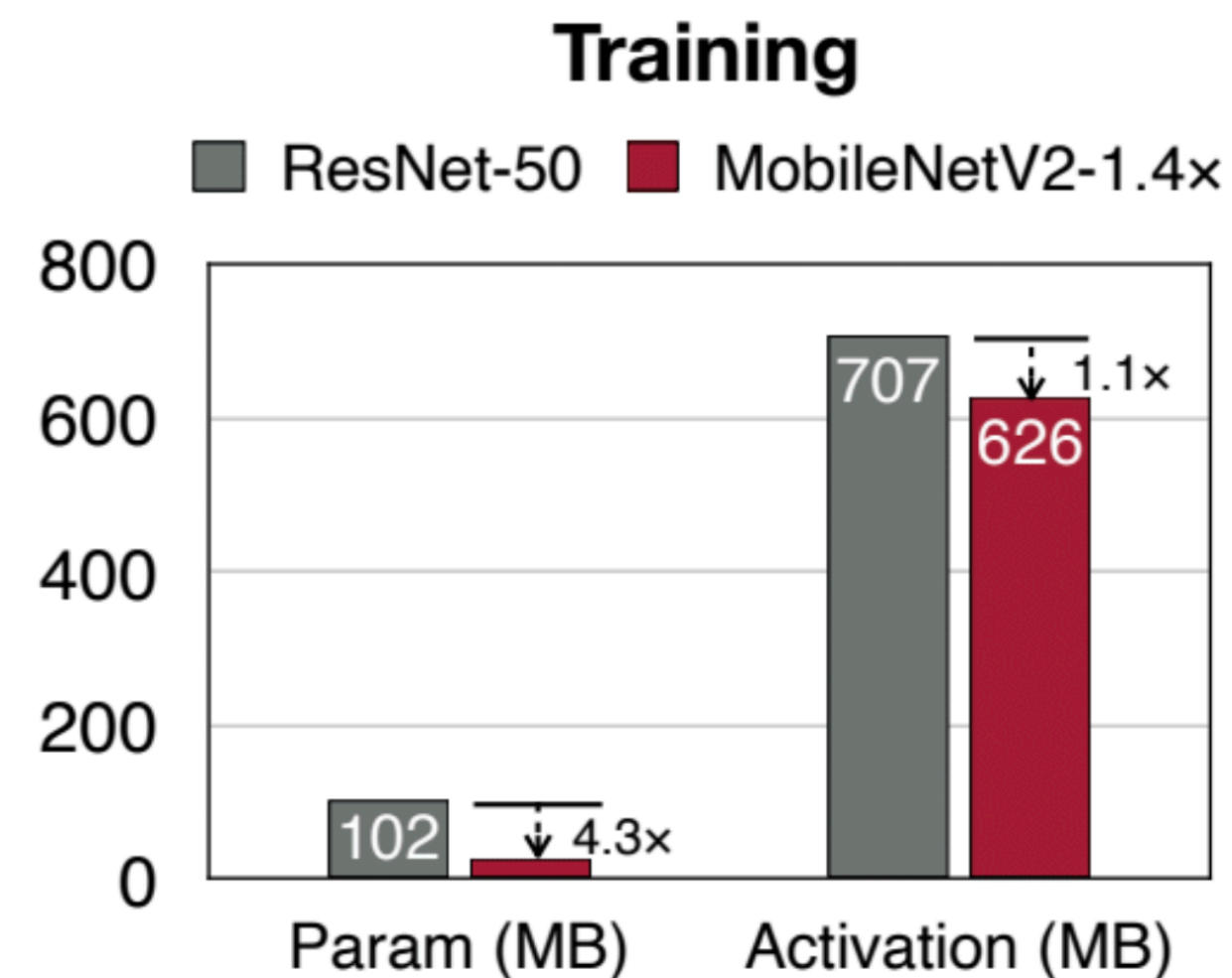
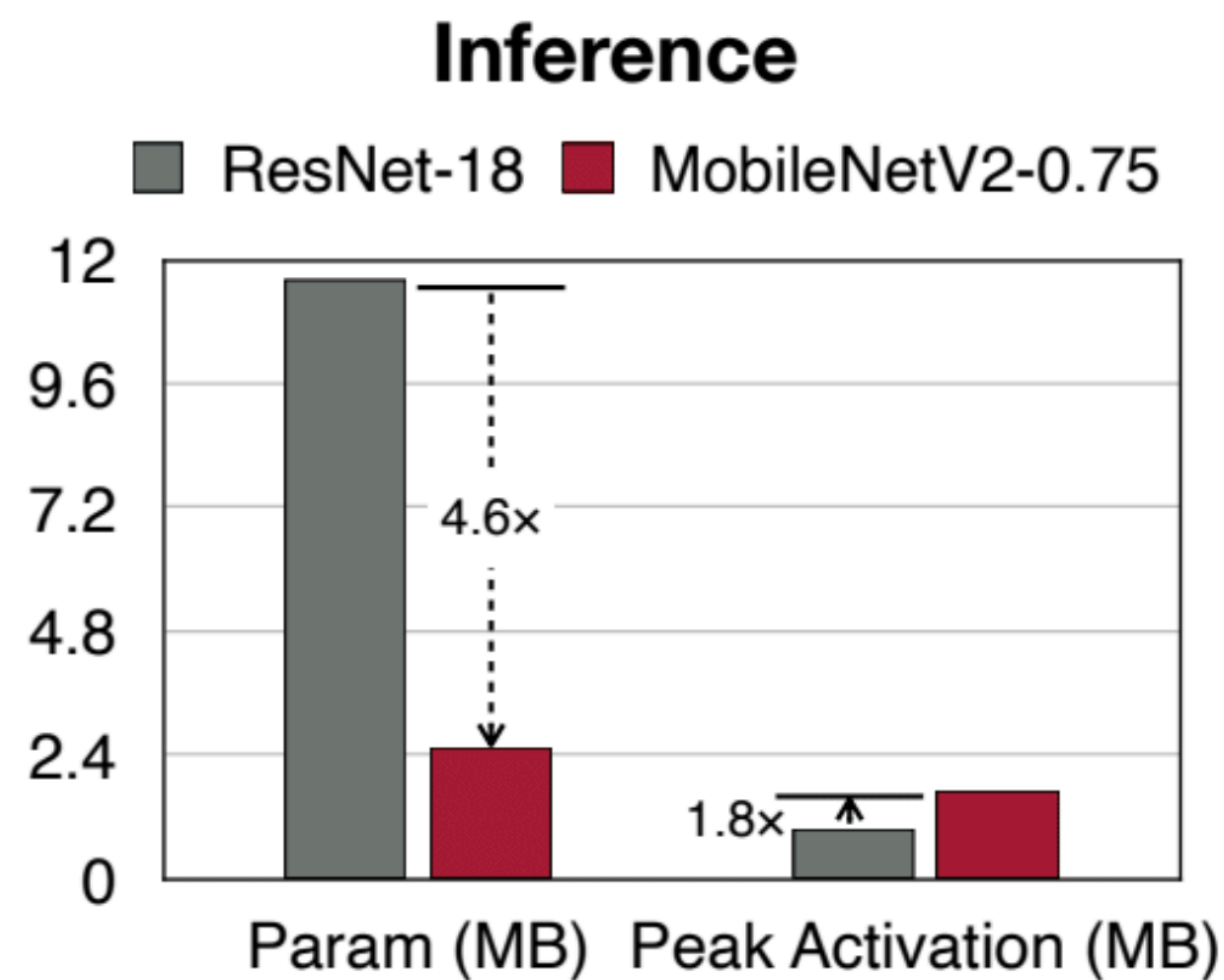
ResNeXT: Grouped bottlenecks

- Combine bottleneck with grouped convolution
 - Equivalent to a multi-path block



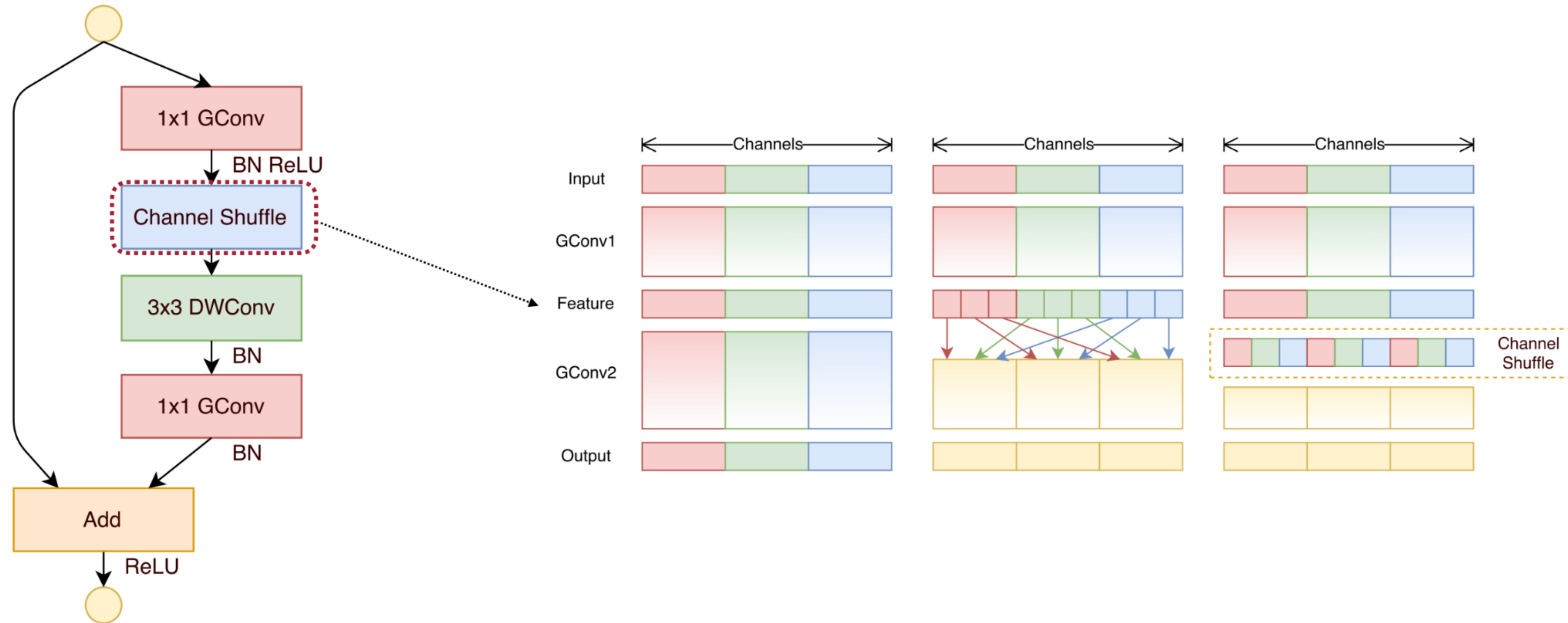
MobileNetv2: Inverted Bottleneck

- Increase #channels → Depthwise convolution → Decrease #Channels
 - Works better than simple depthwise + 1x1 without channel inflation
- **Drawback.** Much activation memory



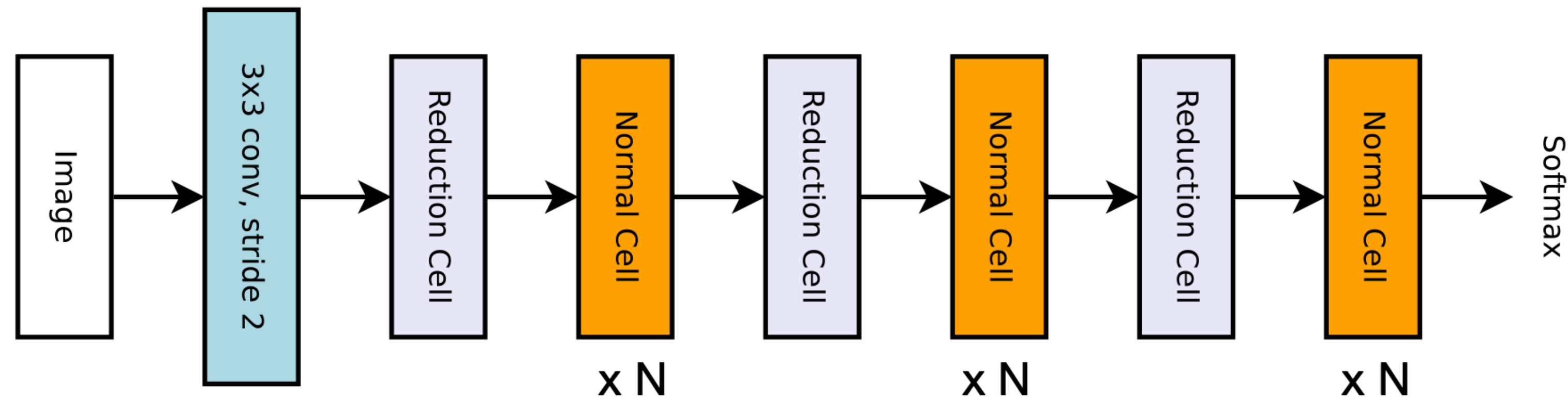
ShuffleNet: Inverted Bottleneck

- Replace 1x1 conv with 1x1 grouped convolution
 - Then, do channel shuffling



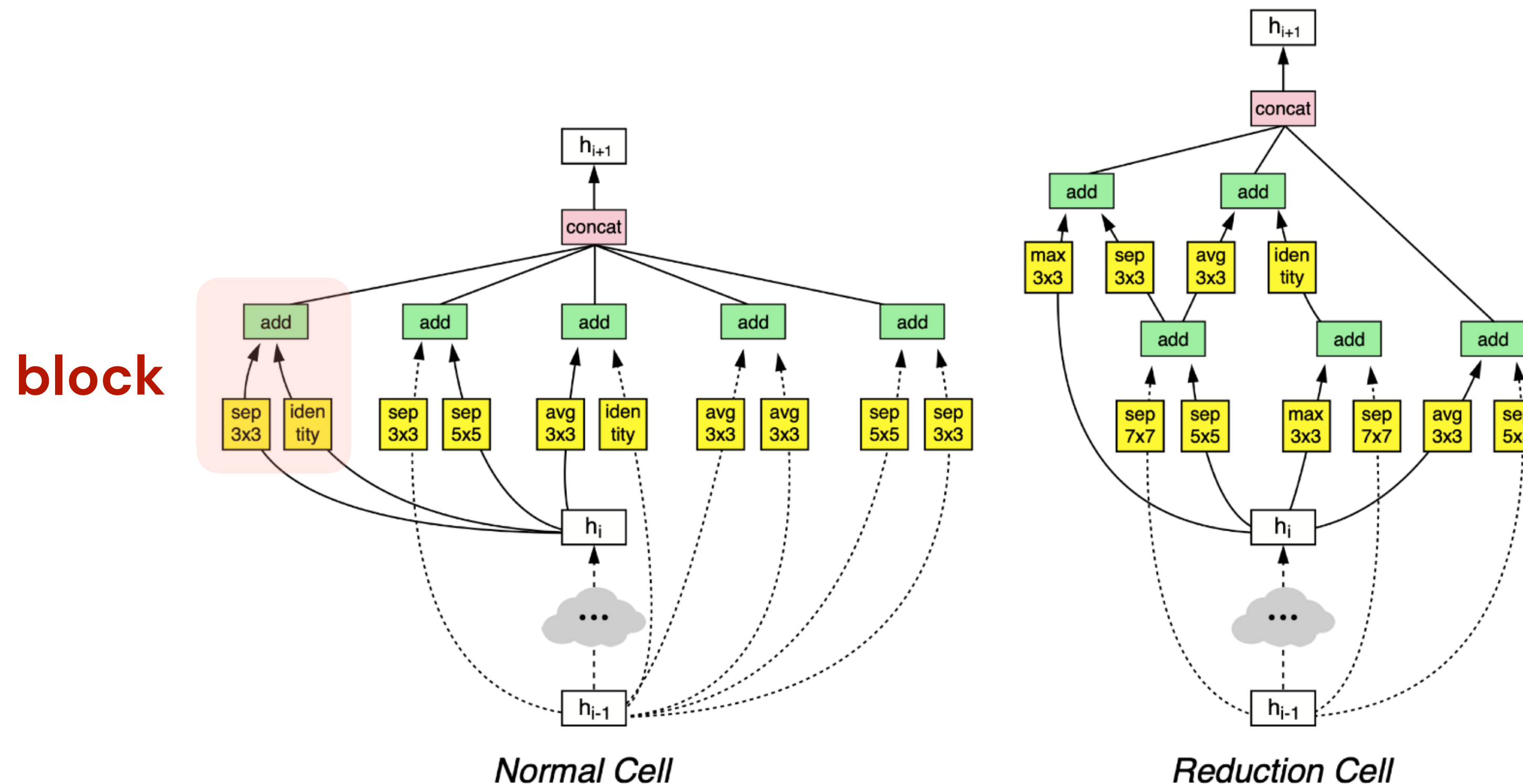
Building the search space

- For image-processing units, typically use **cell-based representation**
 - We describe the approach in NASNet
- A net consists of **repeated cells** + reduction cells (downsampling)
 - Inspired by successful models
 - Reduced search space



Building the search space

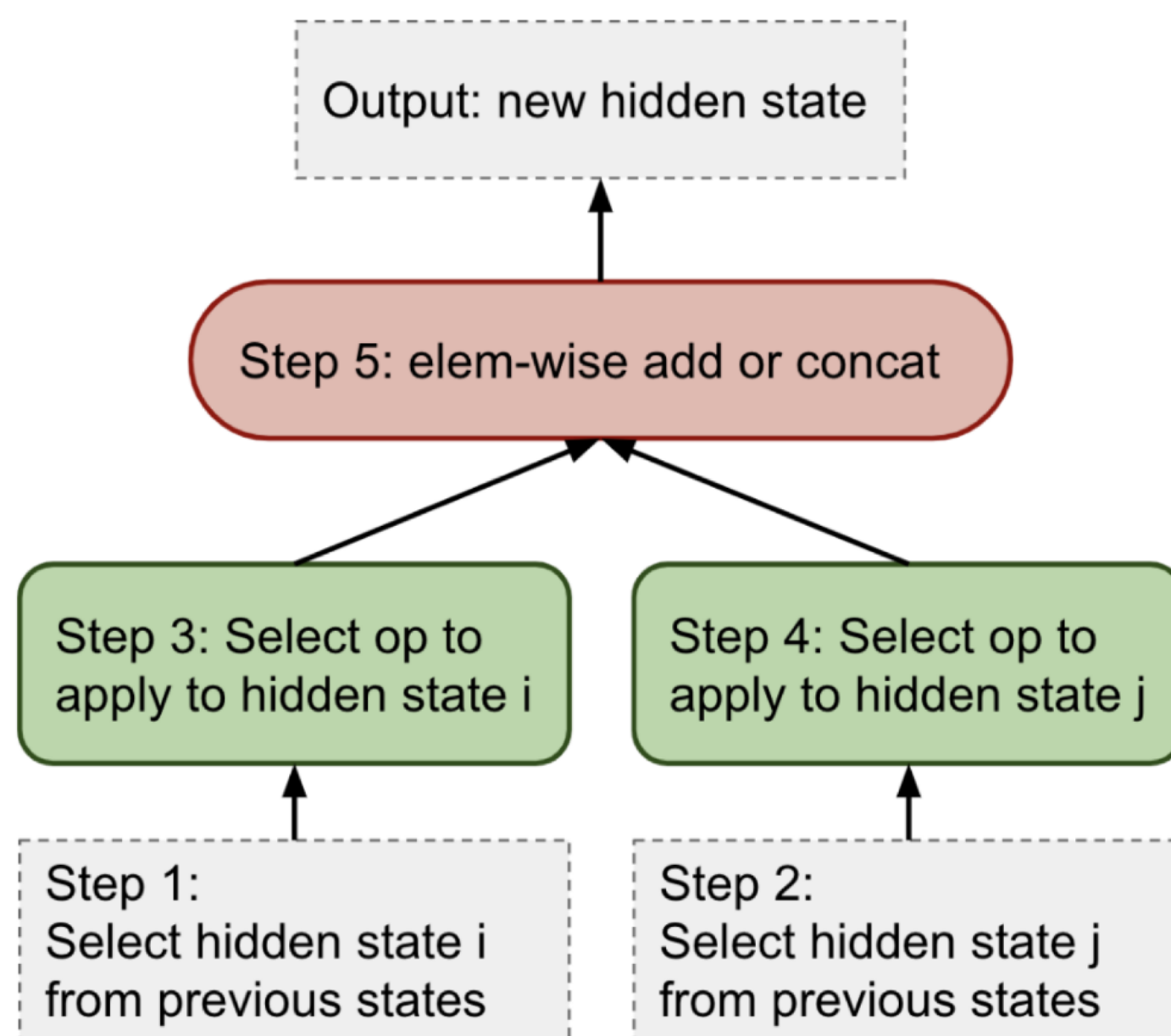
- A cell consist of **multiple blocks**
 - Placed in parallel, or in series
 - Example. NASNet searched on CIFAR-10, set to have five blocks



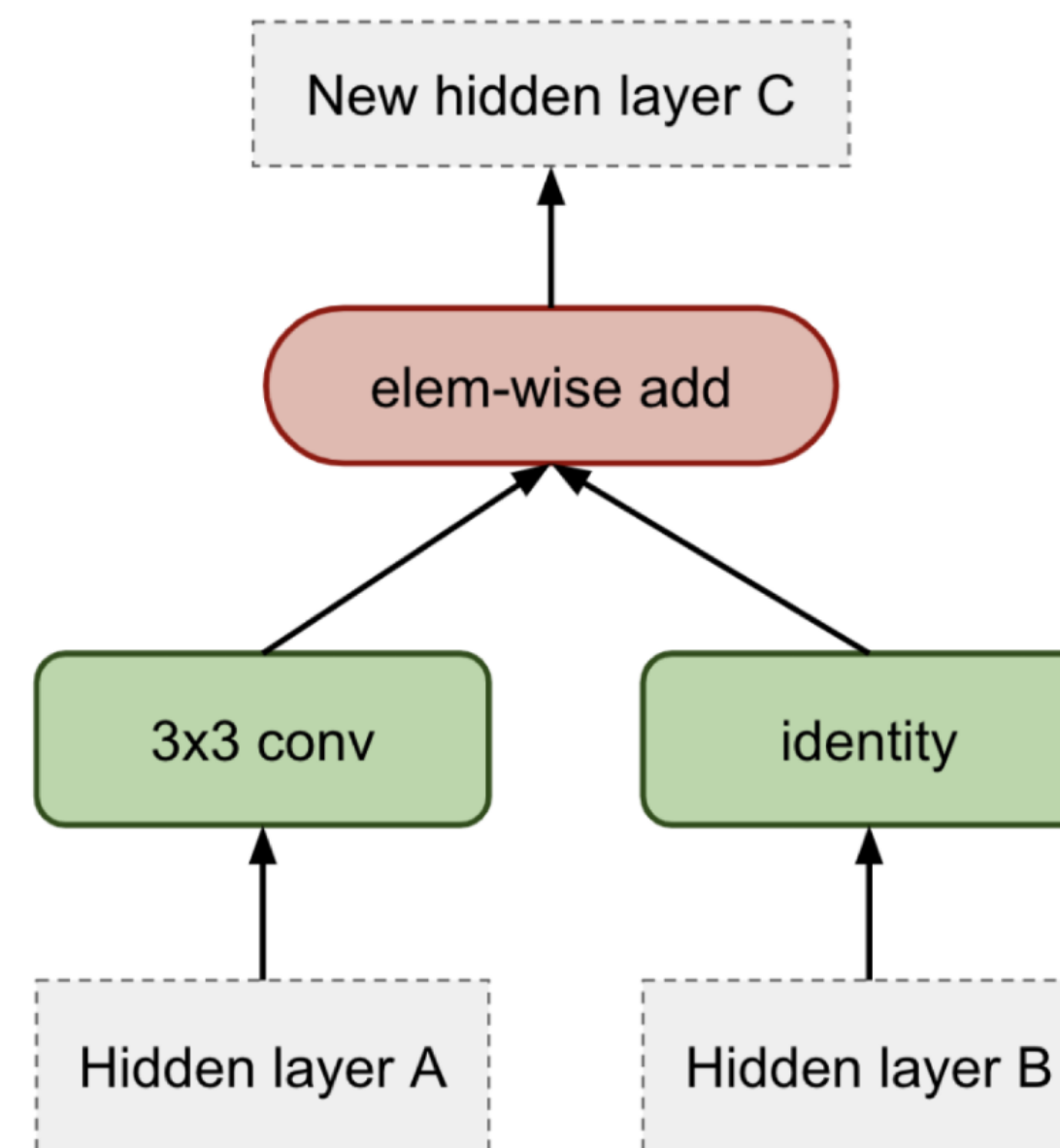
Building the search space

- A block consist of **five discrete choices**
 - Select inputs, process, aggregate
 - Processing ops are pre-handpicked (\Rightarrow)

- identity
- 1x7 then 7x1 convolution
- 3x3 average pooling
- 5x5 max pooling
- 1x1 convolution
- 3x3 depthwise-separable conv
- 7x7 depthwise-separable conv
- 1x3 then 3x1 convolution
- 3x3 dilated convolution
- 3x3 max pooling
- 7x7 max pooling
- 3x3 convolution
- 5x5 depthwise-seperable conv



(a) 5 discrete choices in each block



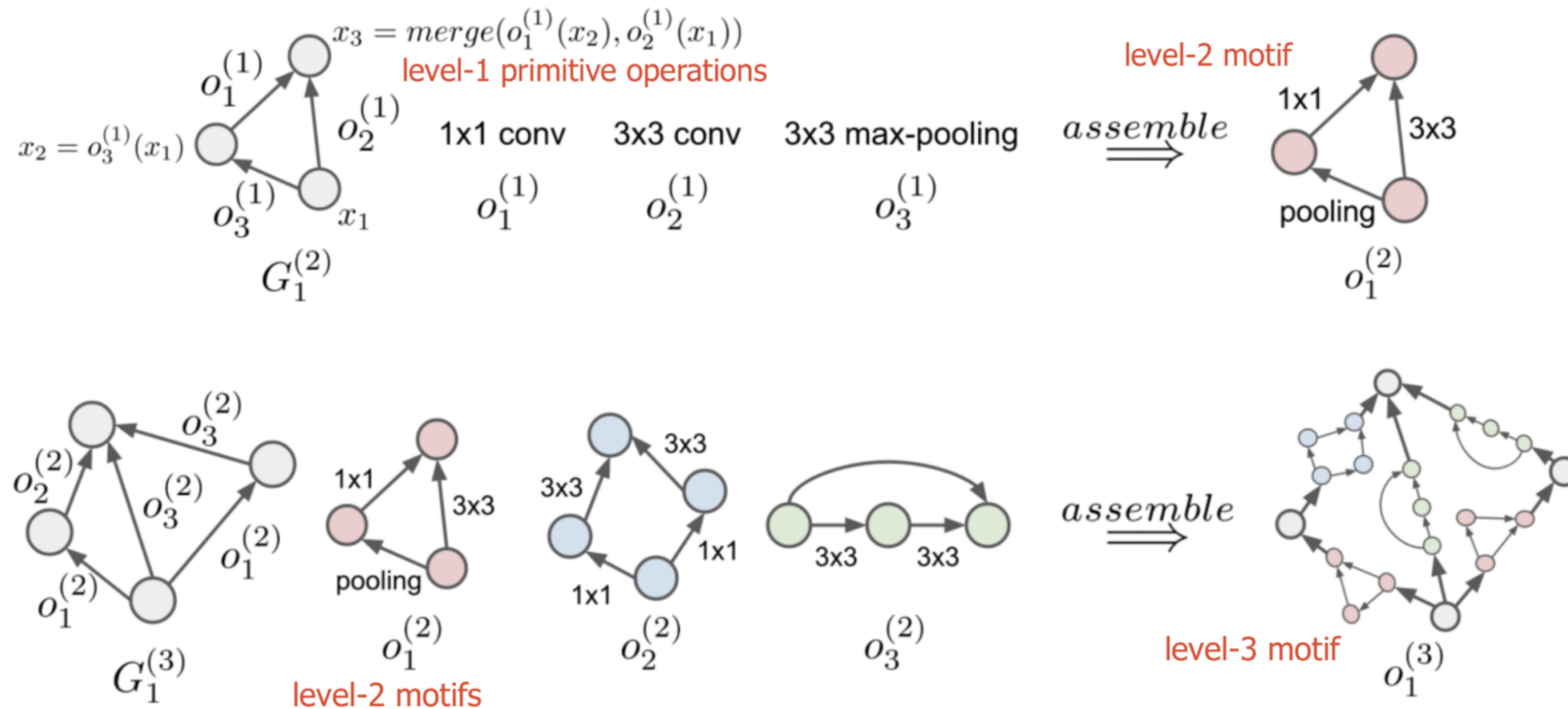
(b) A concrete example

Extending the search space

- Note that we made several arbitrary choices:
 - Number of cell repetitions
 - Kernel size
 - Degrees of downsampling
 - Input resolution
 - (...)
- These were also searched in later works
 - e.g., MNASNet, RegNet, ProxylessNAS, OFANet

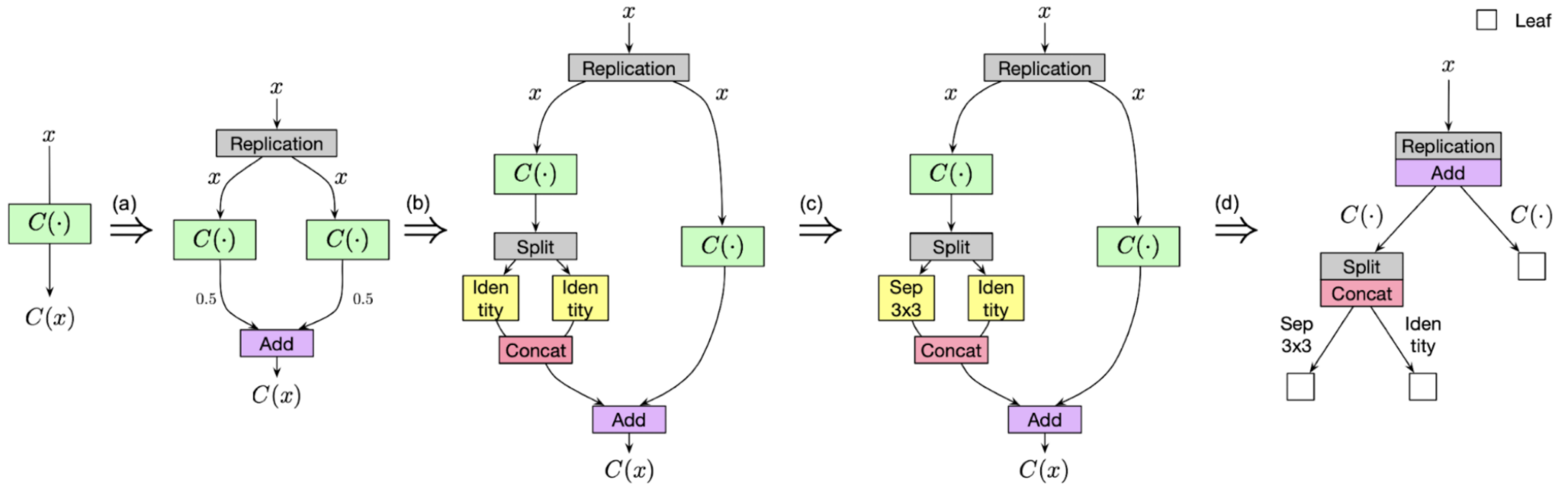
Extending the search space

- Some works proposed more complicated structures than repeated cells
 - Example. Hierarchical NAS



Extending the search space

- Example. Tree-like branching structures



Search strategy

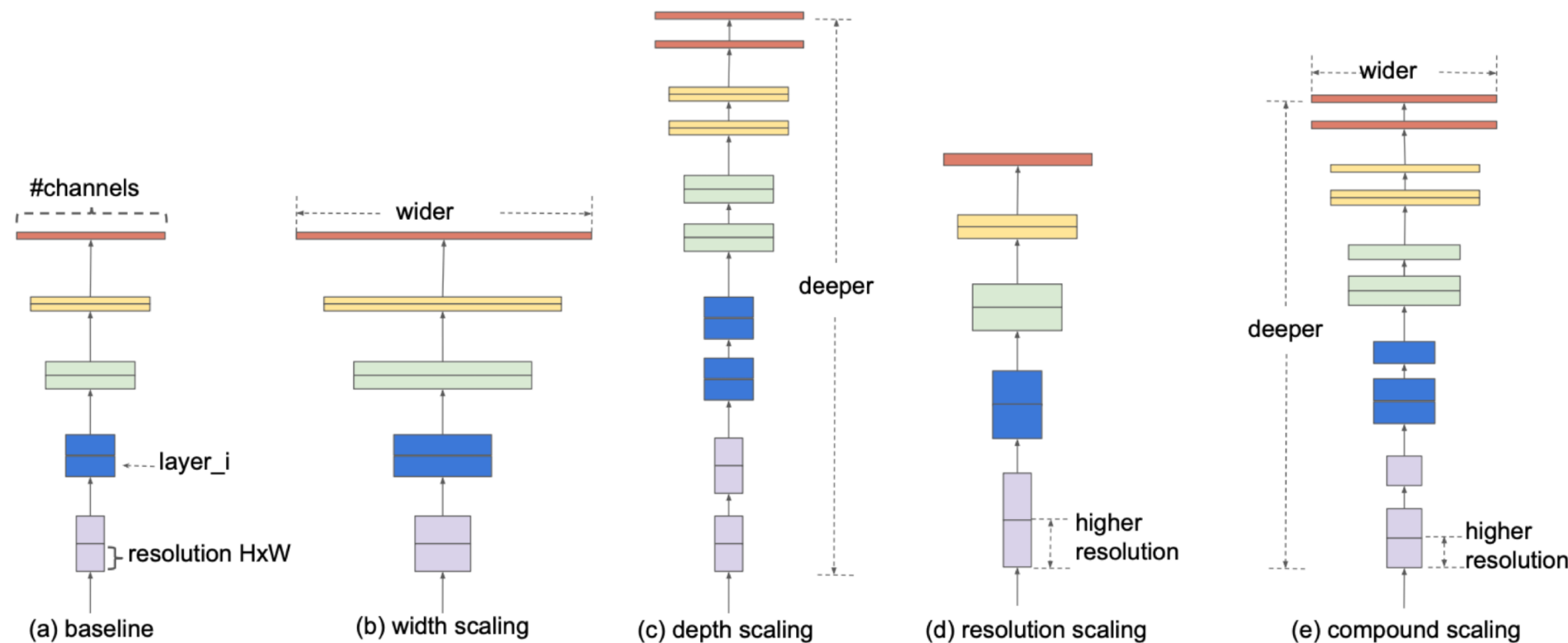
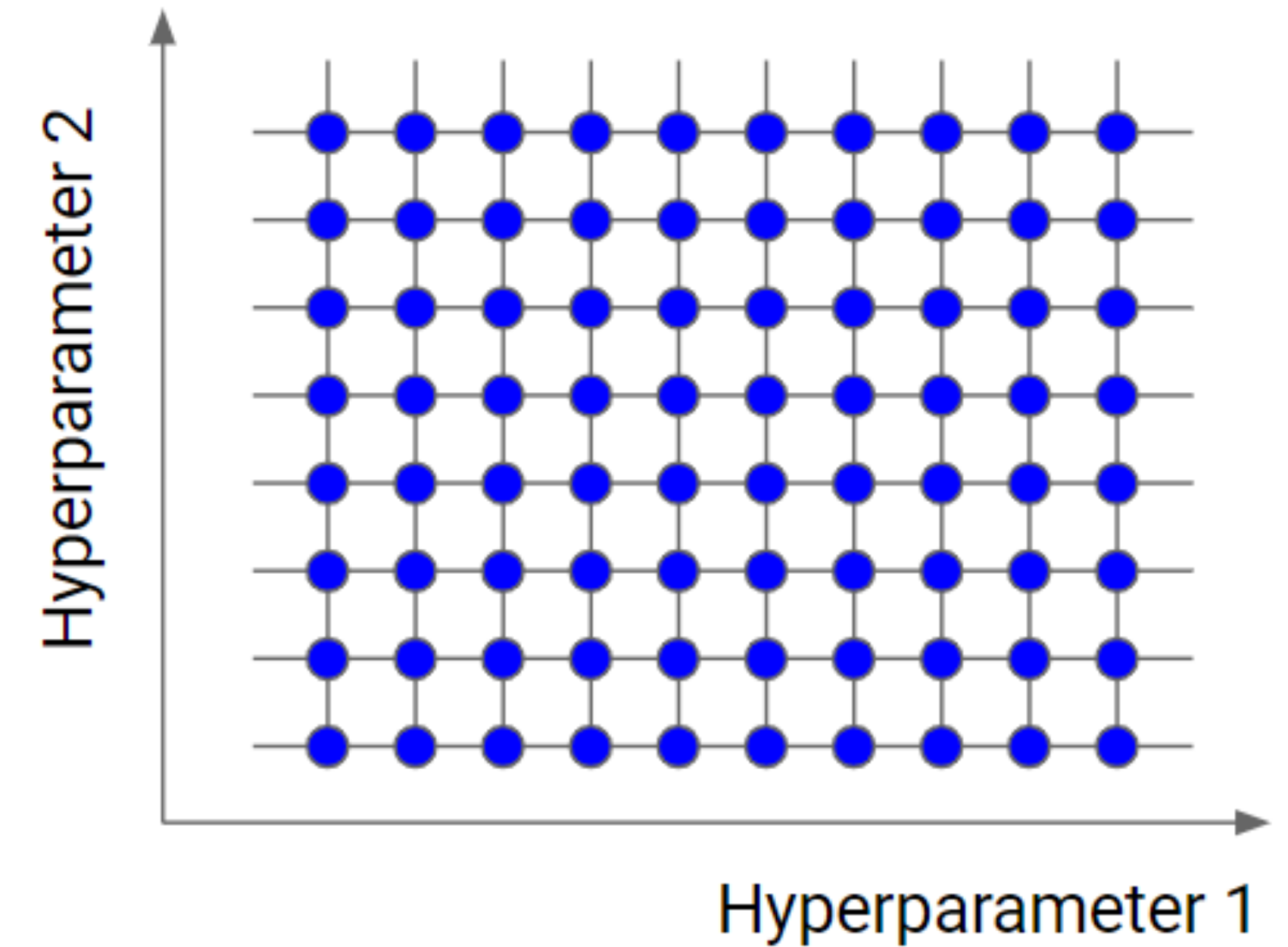
Searching

$$\min_{a \in \mathcal{A}} \ell(a)$$

- **Problem.** Searching over **discrete** space
 - Grid / random search
 - Reinforcement learning
 - Evolutionary method
 - Progressive search
- Differentiable options \Leftarrow discussed in the next section

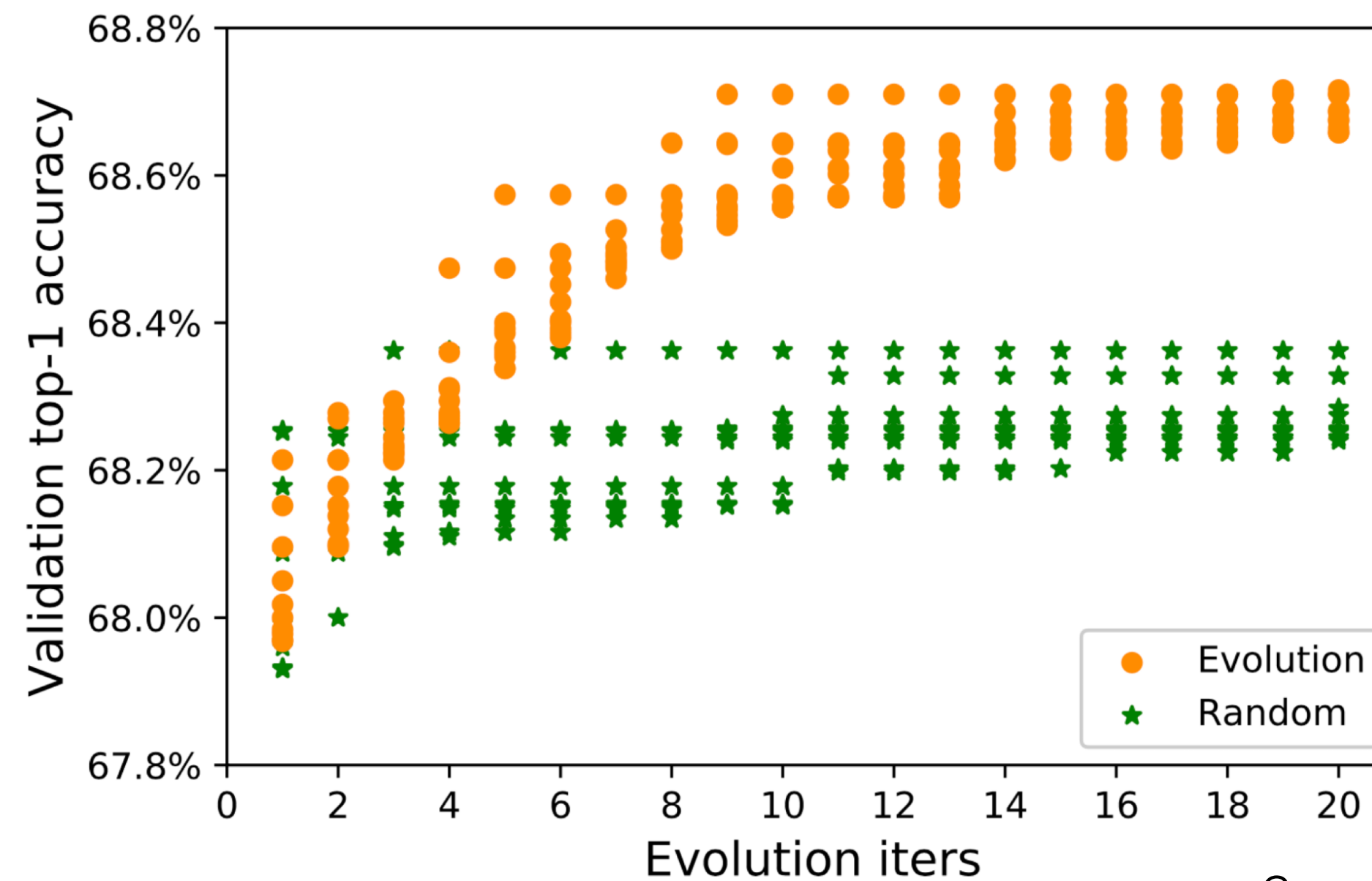
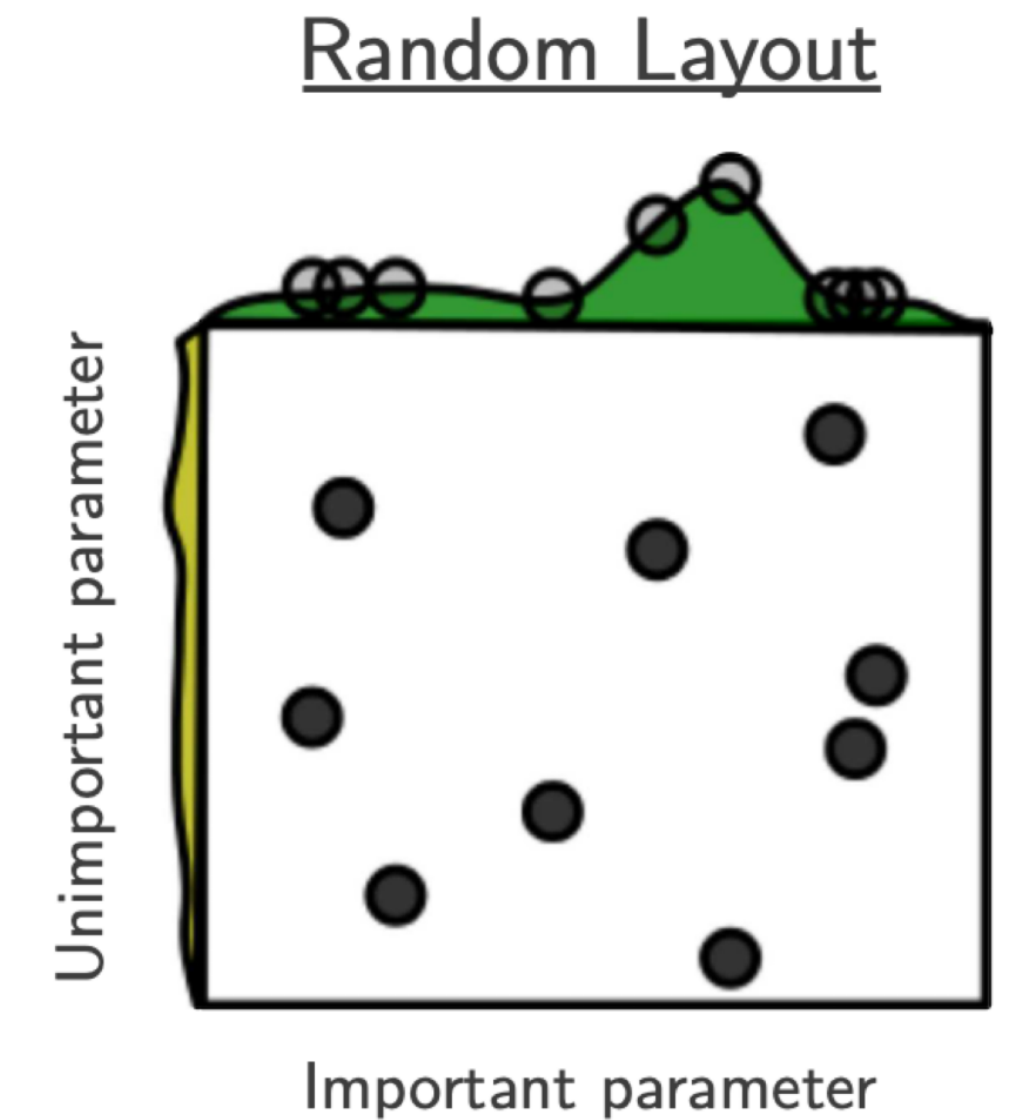
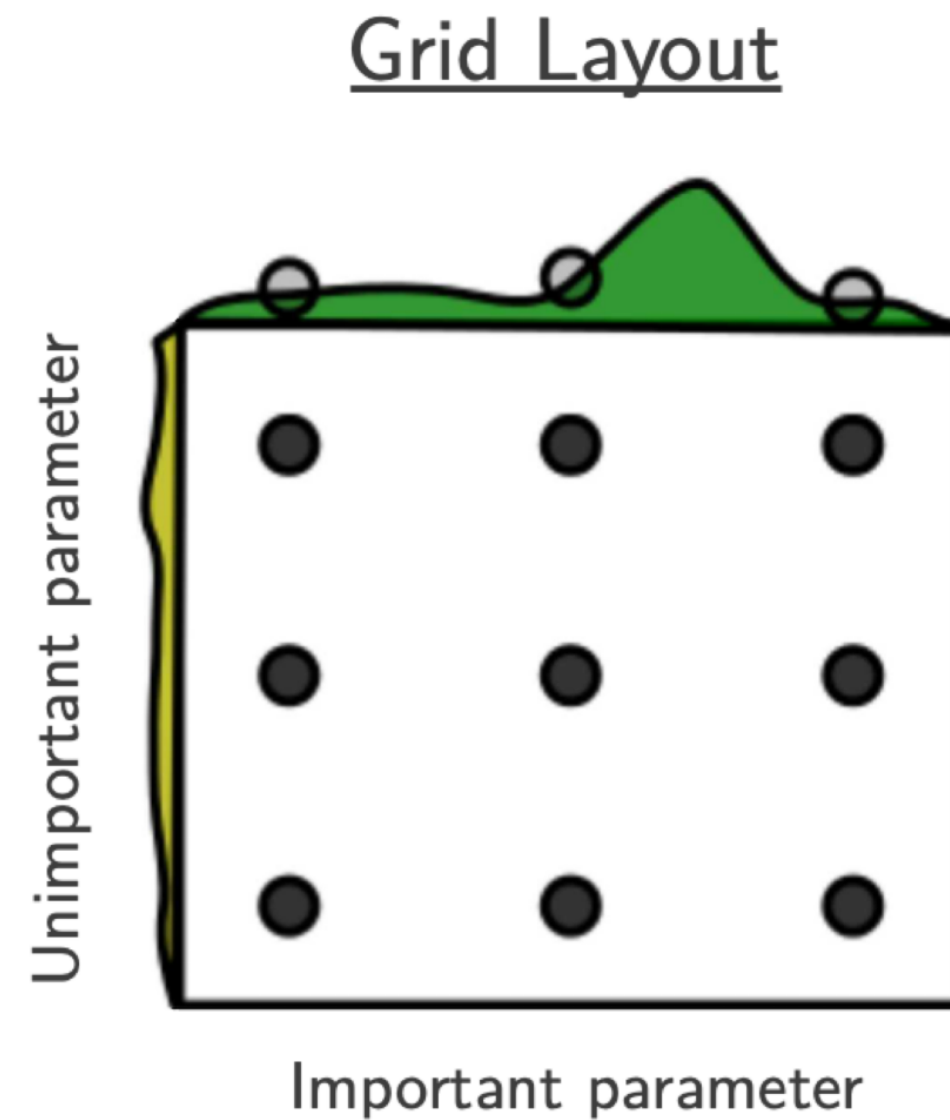
Grid Search

- Simply list all possible choices
 - Exponential growth in scale
 - Can be used for extremely simplified search space
 - e.g., EfficientNet



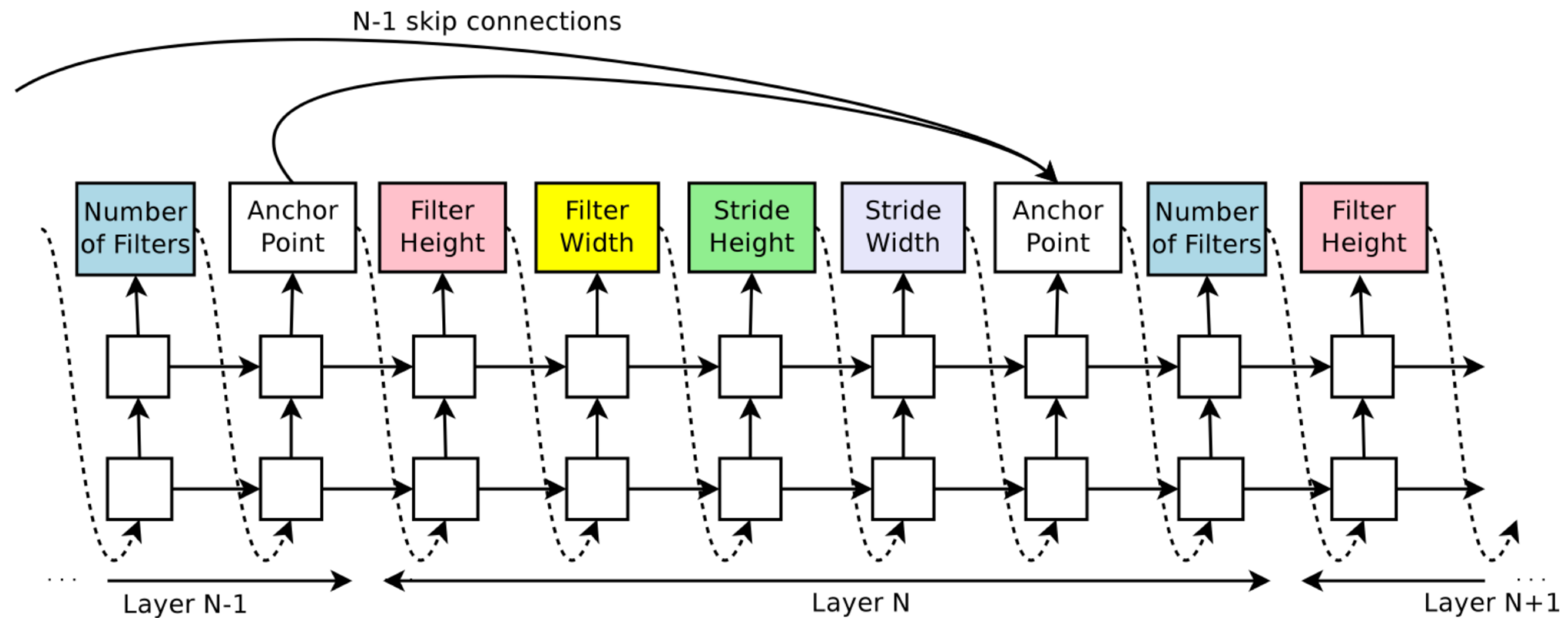
Random Search

- More effective utilization of trials
 - With grid search, effective number of samples is 3
 - Very simple, but effective



Reinforcement learning

- Train a **policy** which generates hyperparameters sequentially
 - Update policy parameters, based on reward
 - Example. Zoph and Le (2017) uses an RNN controller



Reinforcement learning

- **Training.** Evaluate policy gradient with respect to the **REINFORCE loss**
(later works used PPO, Q Learning, MTCS, ...)

- Given the model parameter θ , RNN generates HPs with distribution

$$p_{\theta}(a_{1:T})$$

- Want-to-do. Maximize the expected reward

$$J(\theta) = \mathbb{E}_{p_{\theta}}[R]$$

- R is the validation accuracy of the model configured by $a_{1:T}$

Reinforcement Learning

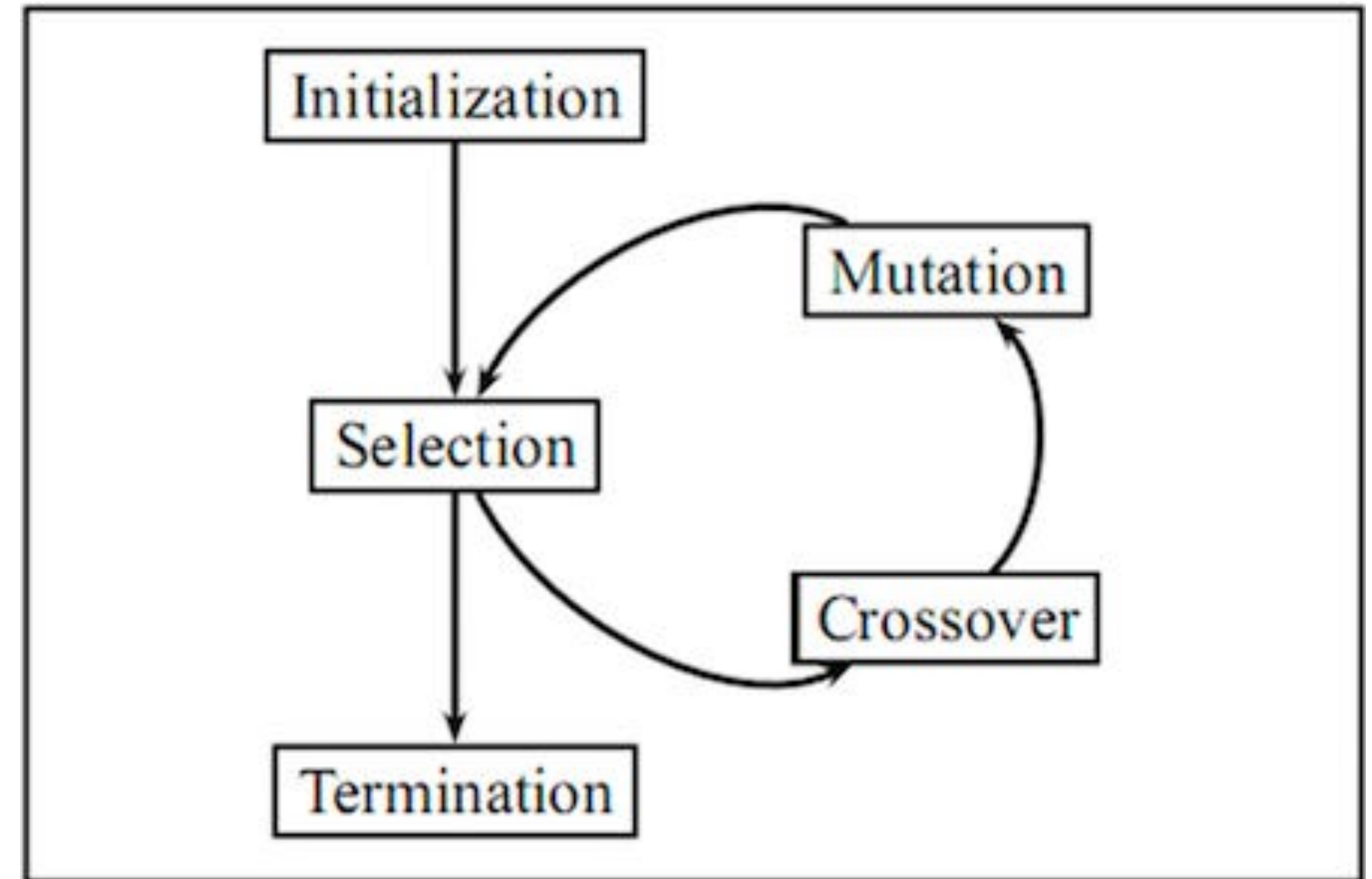
- Update RNN controllers using the gradient:

$$\begin{aligned}\nabla_{\theta} J(\theta) &= \nabla_{\theta} \int \left(\prod_{t=1}^T p_{\theta}(a_t | a_{1:t-1}) \cdot R \right) da_{1:T} \\ &= \int \left(\sum_{t=1}^T \frac{\nabla_{\theta} p_{\theta}(a_t | a_{1:t-1})}{p_{\theta}(a_t | a_{1:t-1})} \cdot p_{\theta}(a_{1:T}) \cdot R \right) da_{1:T} \\ &= \sum_{t=1}^T \mathbb{E} [\nabla_{\theta} \log p_{\theta}(a_t | a_{1:t-1}) \cdot R]\end{aligned}$$

- If R was high, strong positive feedback to generate similar HPs
- If R was low, weak positive feedback (thus called “reinforce,” not penalize)

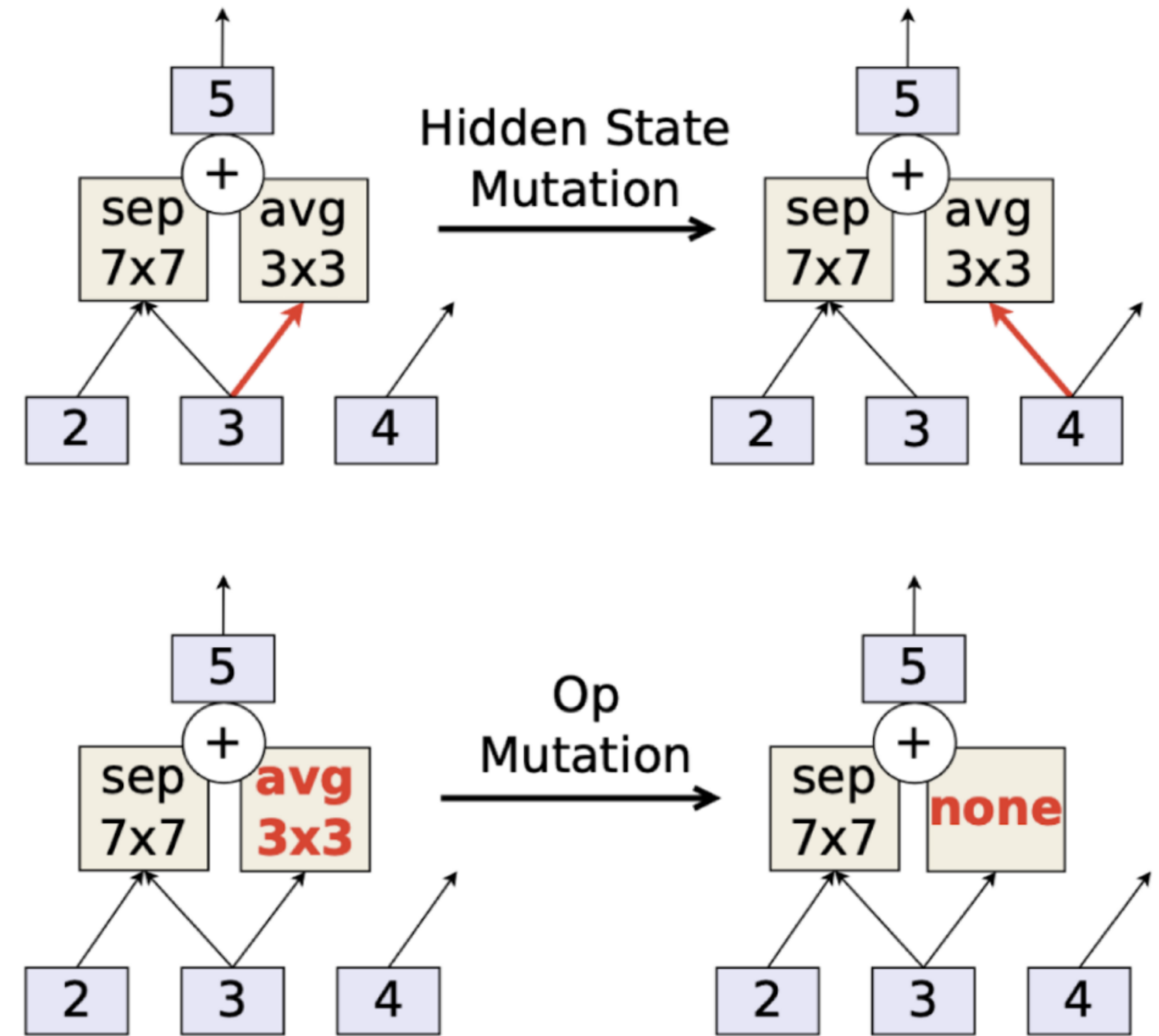
Evolutionary method

- Do the following:
 - Start from a set of solutions
 - Repeat:
 - Pick a solution
 - Randomly mutate it
 - If good, add it to population (optionally, remove one)



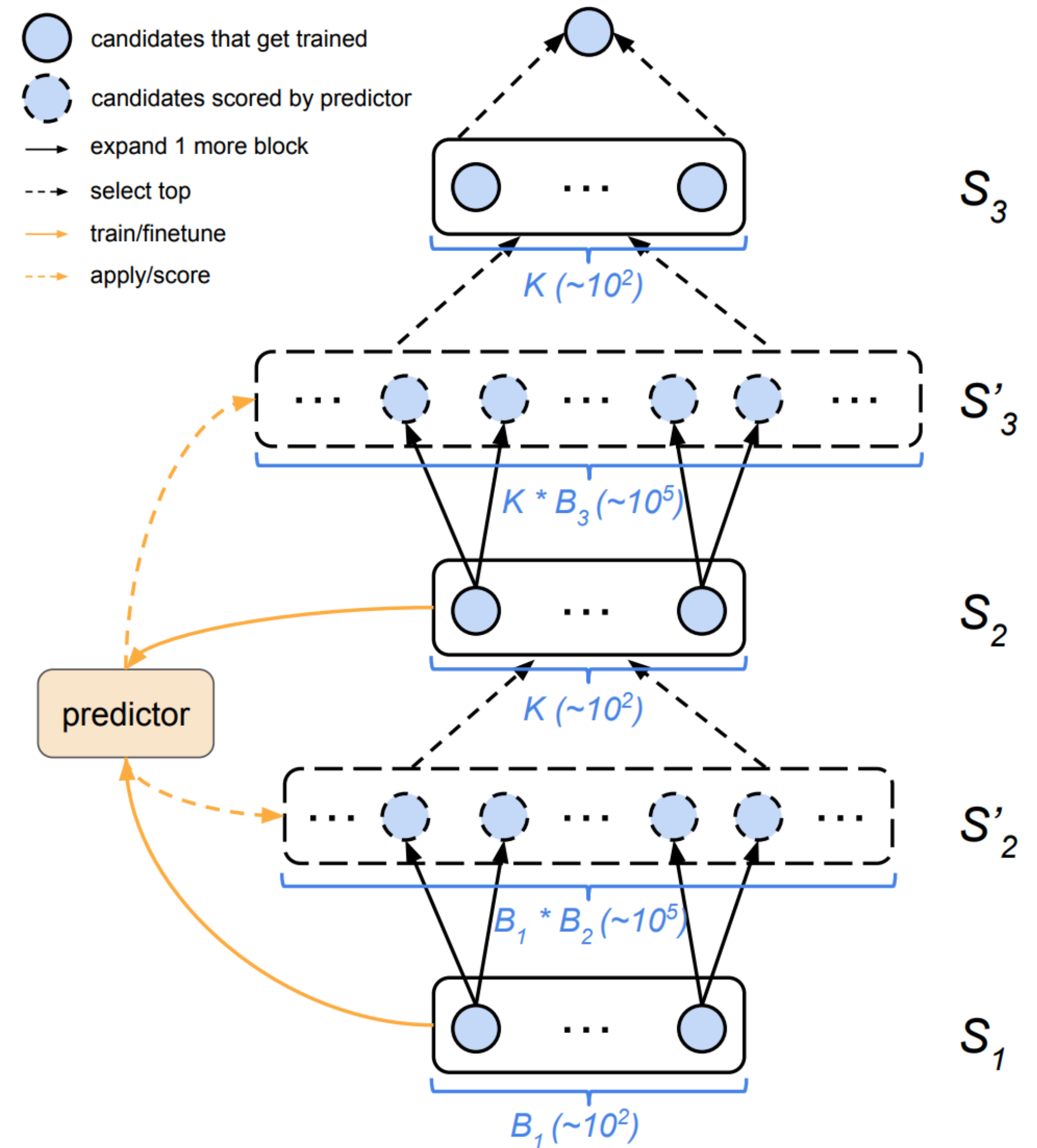
Evolutionary method

- Example. AmoebaNet
- Uses **tournament selection**
 - Sample S models from the population
 - Pick highest acc. model as parent
 - Mutate parent to get a child
 - Train child and evaluate
 - Add child to the population



Progressive search

- These ideas are often combined with progressive search
- Example. Progressive NAS
 - Search for 1-Block cells
 - Select top-k cells
 - Add one block to top-K cells
 - (repeat)



Evaluation strategy

Evaluation strategy

$$\min_{a \in \mathcal{A}} \ell(a)$$

- **Idea.** Use a cheaper proxy
 - Smaller duration (less epochs)
 - Smaller data (less #data, less resolution)
 - Smaller model (less #channels, less repeated blocks)
- Re-use trained weights
- Joint training

Shorter training

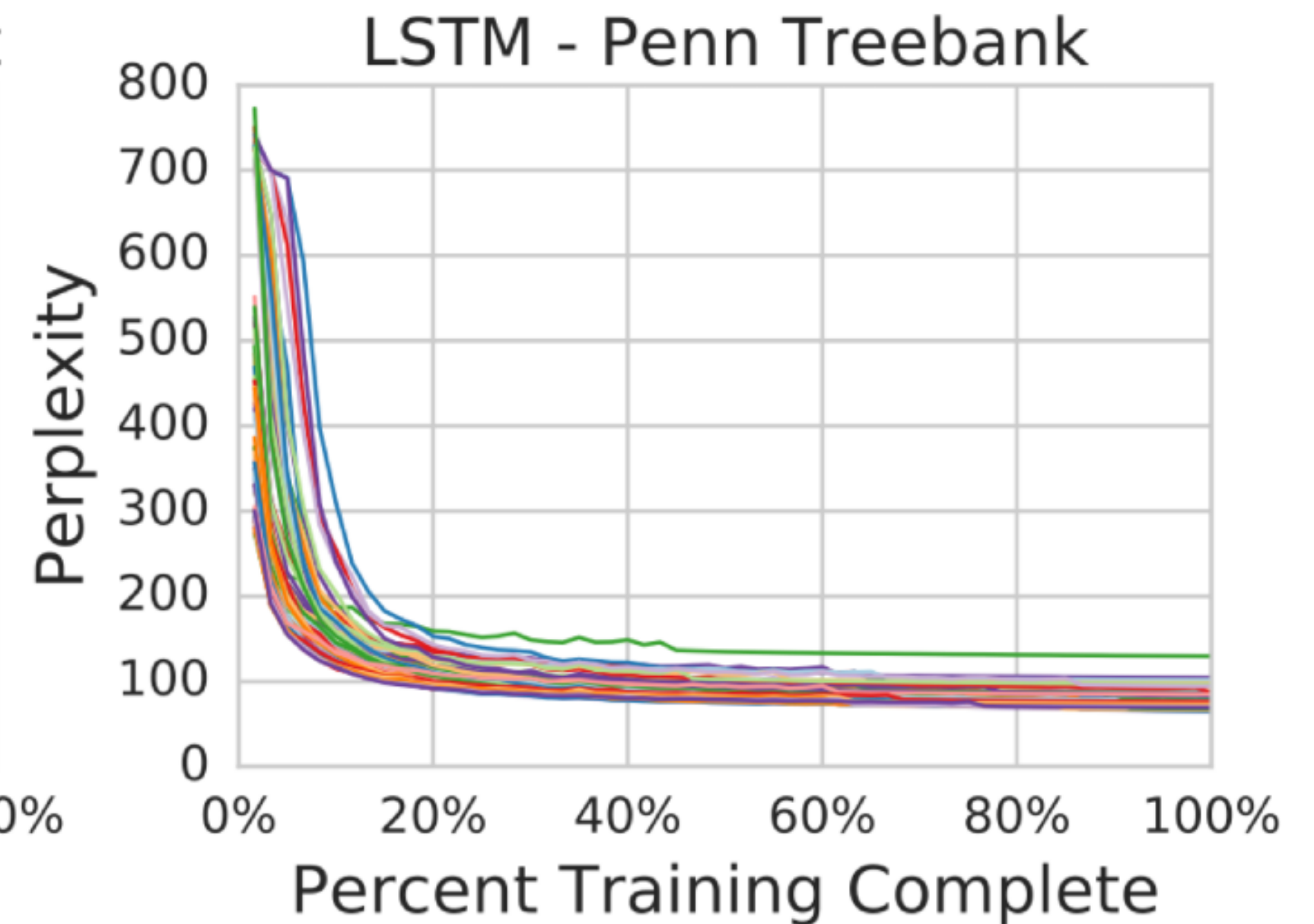
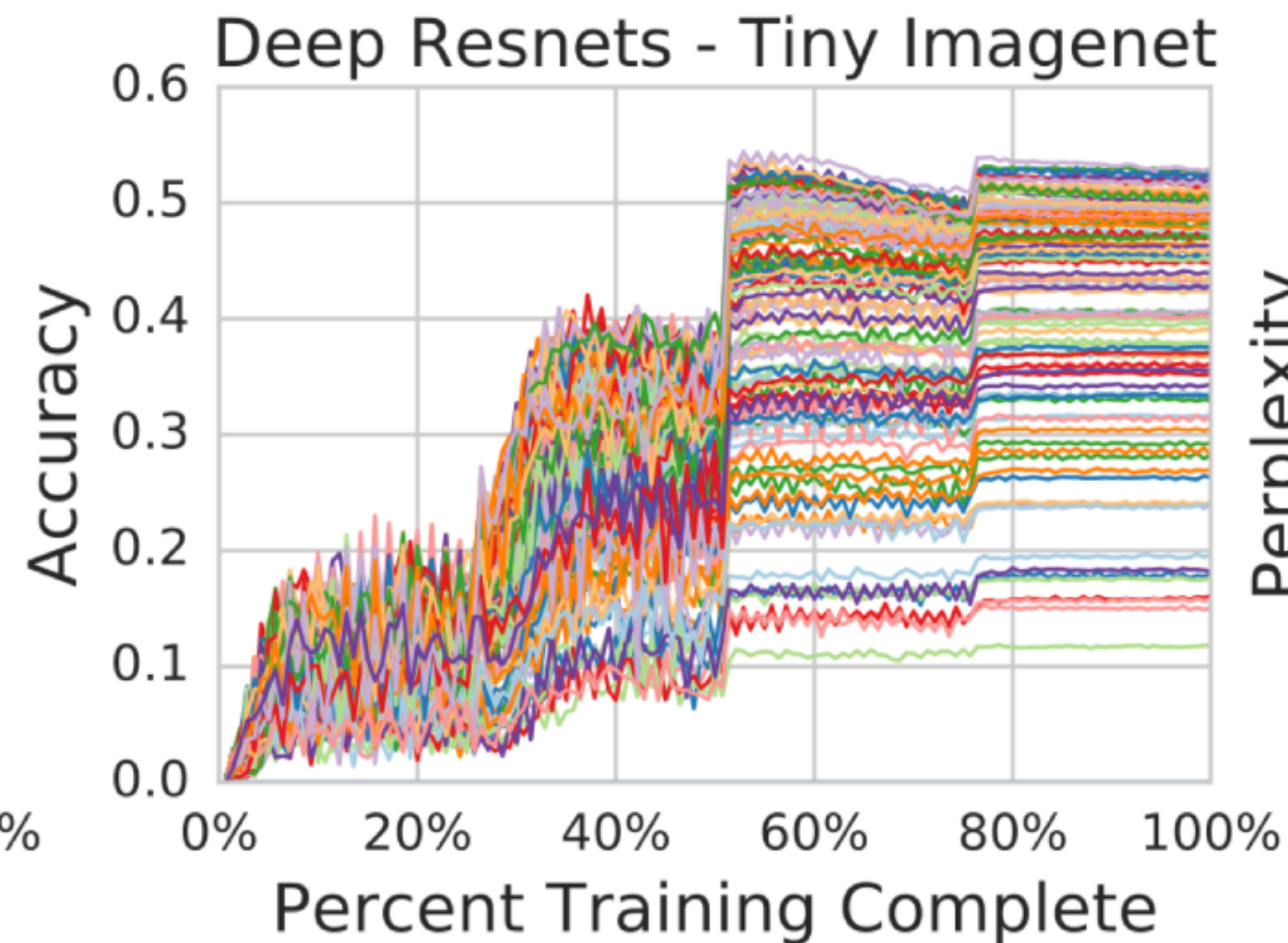
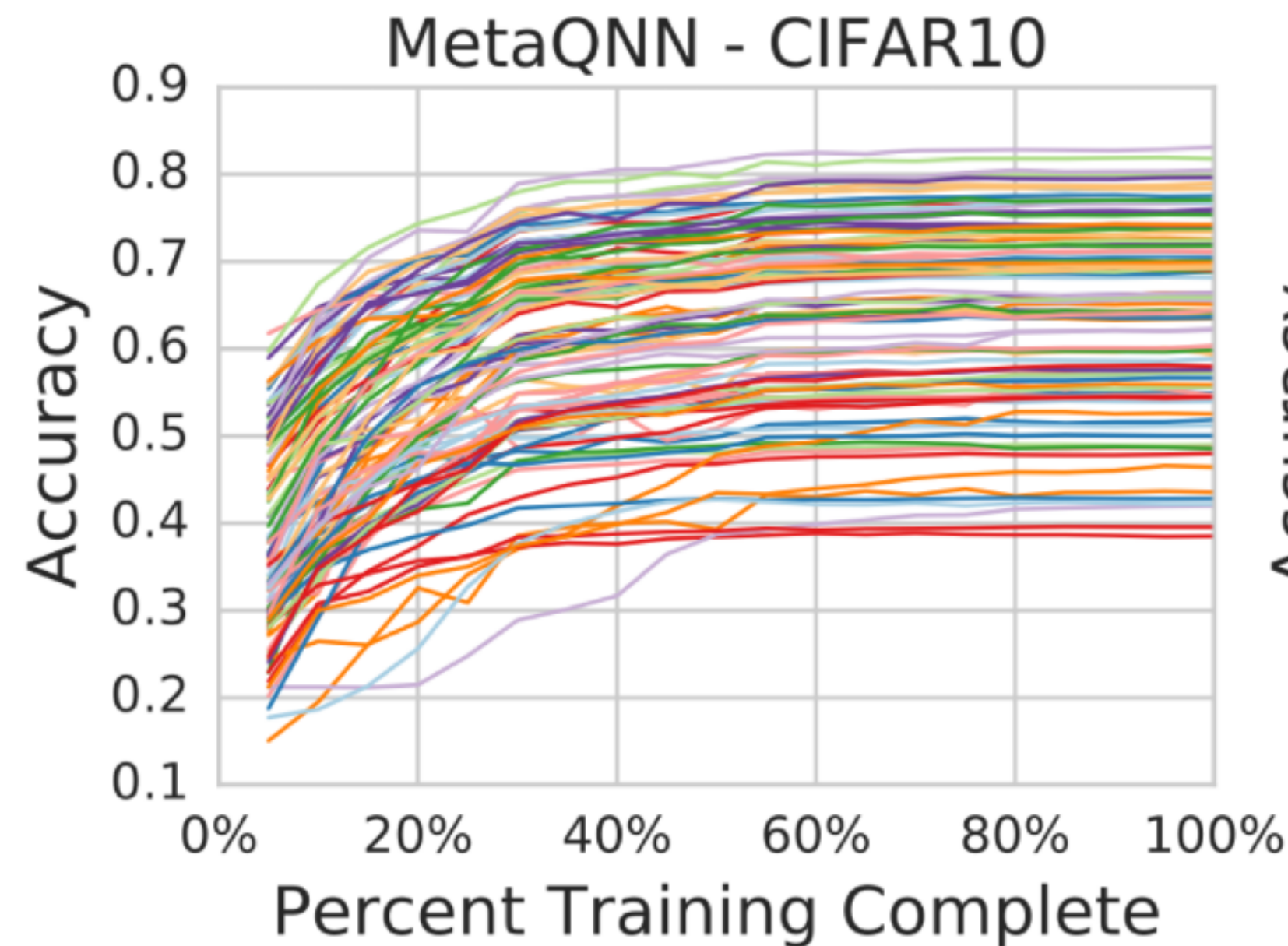
- **Problem.** Simply selecting the best solution may not be good enough
 - Poor correlation with final accuracy

Table 1: Spearman rank correlation coefficients of the validation errors between different budgets. The correlation is high between every budget and the next larger one, but degrades quickly beyond that.

	1200s	1h	3h
400s	0.87	0.31	0.05
1200s		0.88	0.64
1h			0.86

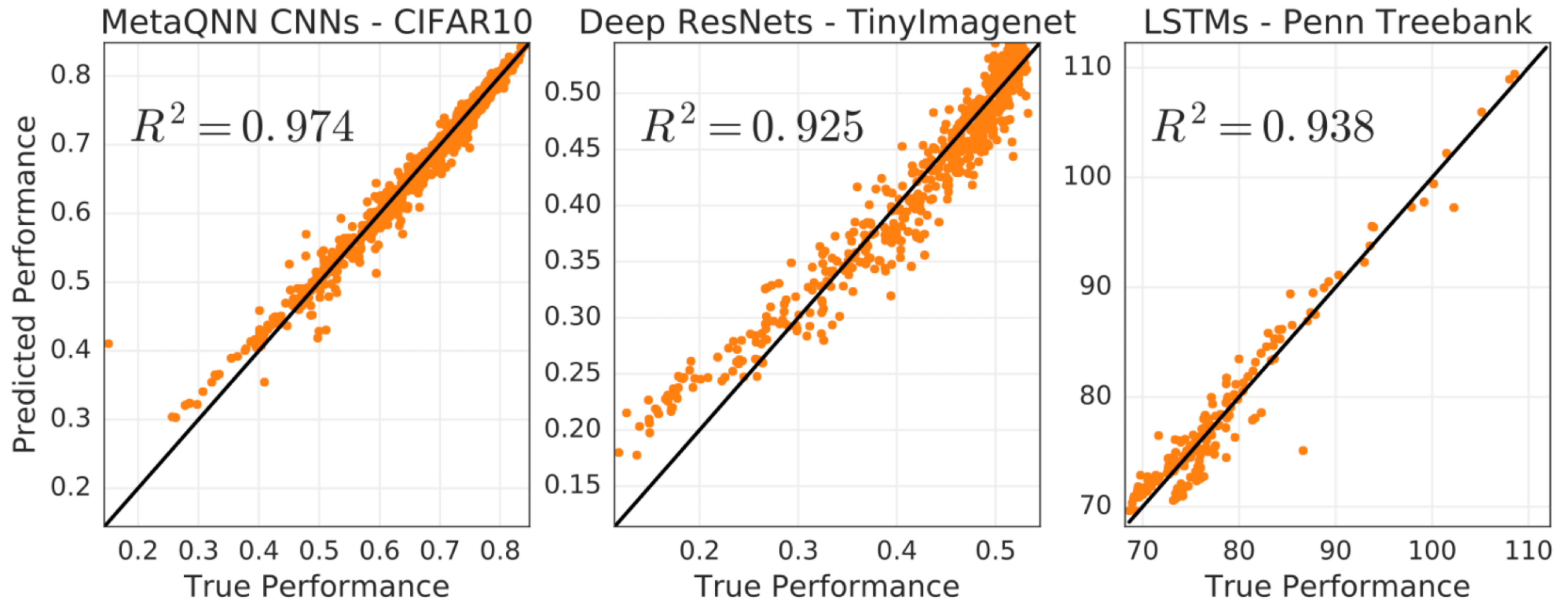
Shorter training

- **Solution.** Train a loss predictor
 - Example. Baker et al. (2018) observes that models have similar loss curves



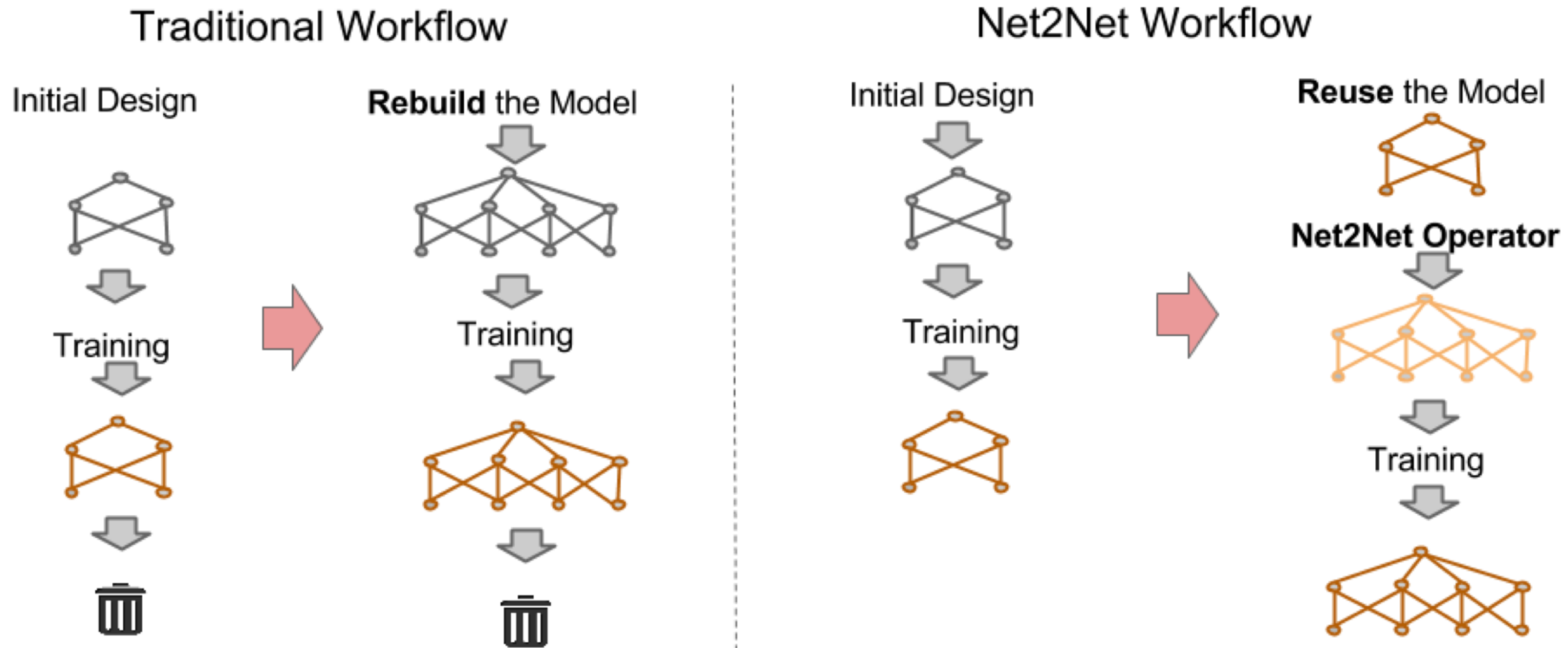
Shorter training

- Baker et al. (2018) used ν -SVR to predict the full curve from the early 25%



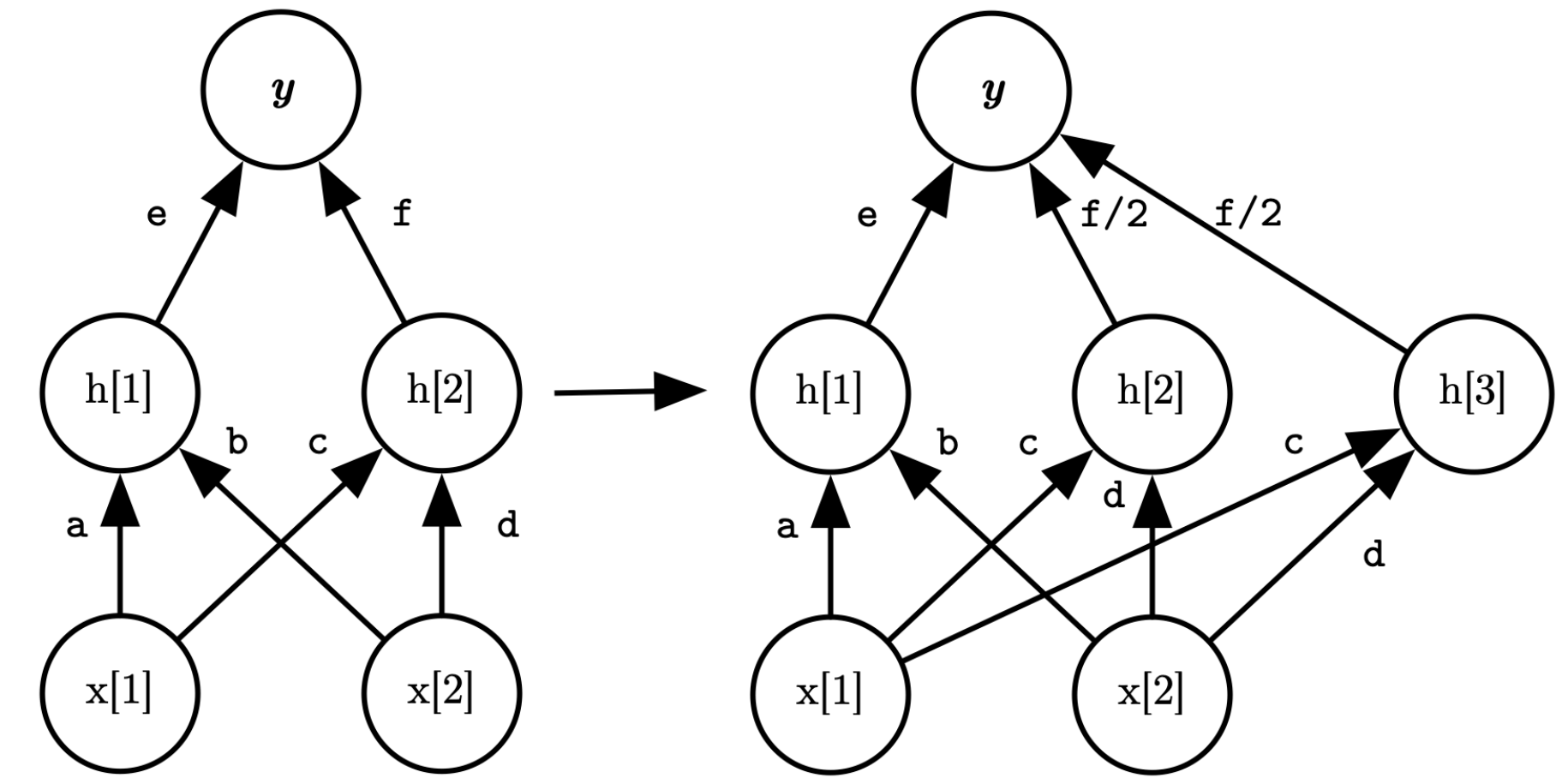
Training re-use

- **Idea.** Reuse the weights trained from prior runs
 - Related. Net2Net (2016) transfers weights to other tasks for adaptation

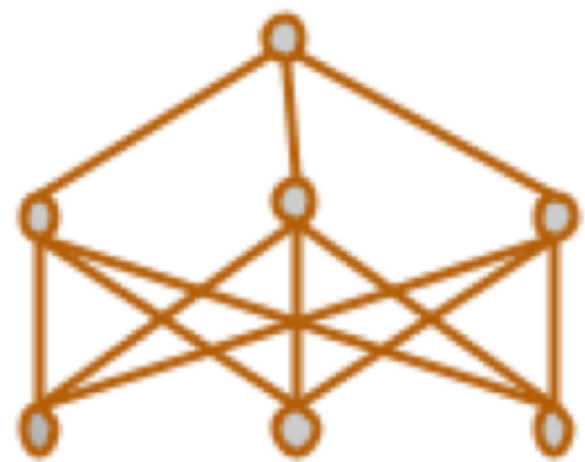


Training re-use

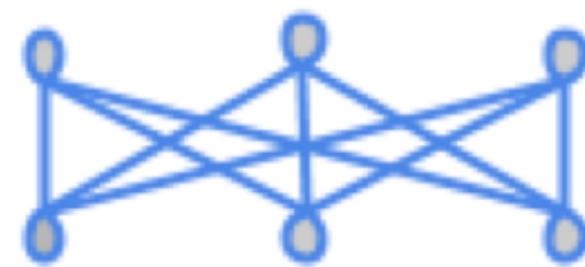
- **Expanding width.** Distribute weights by half
- **Expanding depth.** Identity function



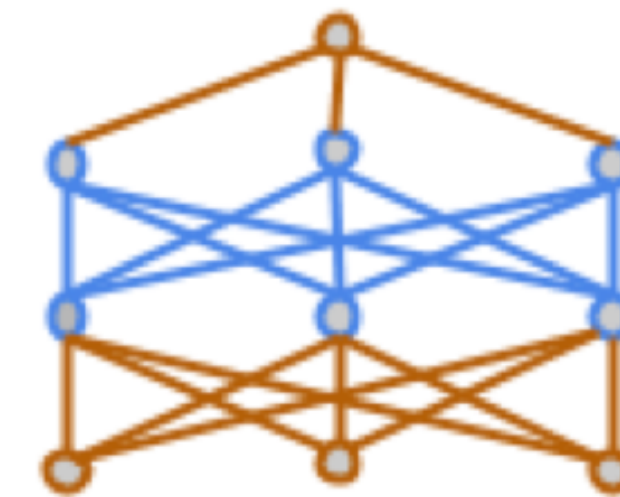
Original Model



Layers that Initialized as Identity Mapping



A Deeper Model Contains Identity Mapping Initialized Layers



Training re-use

- **App. to NAS.** EfficientNAS views NAS as **finding a subgraph** of a giant net
 - Update weights with SGD
 - Select subgraph with RNN

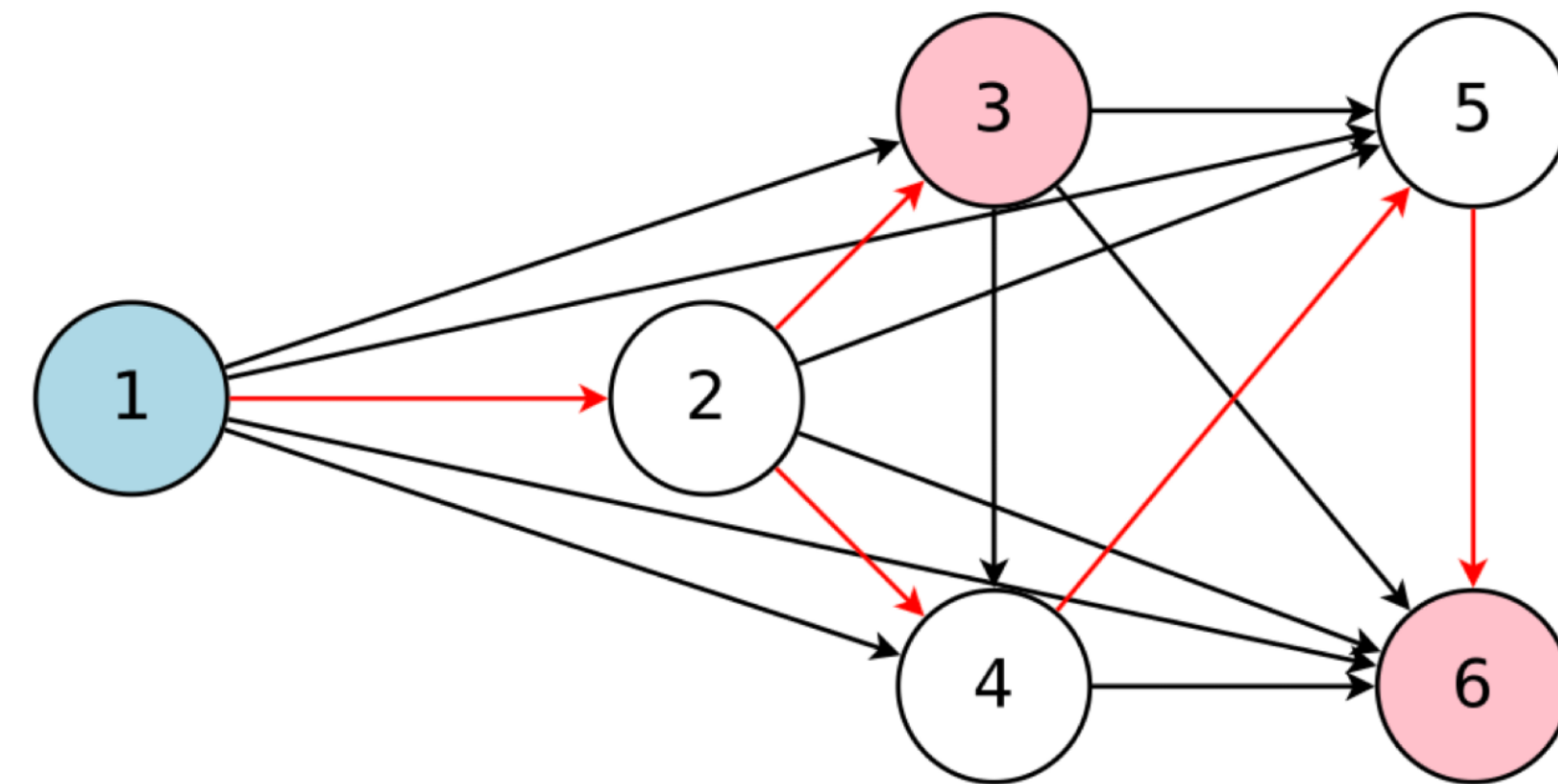
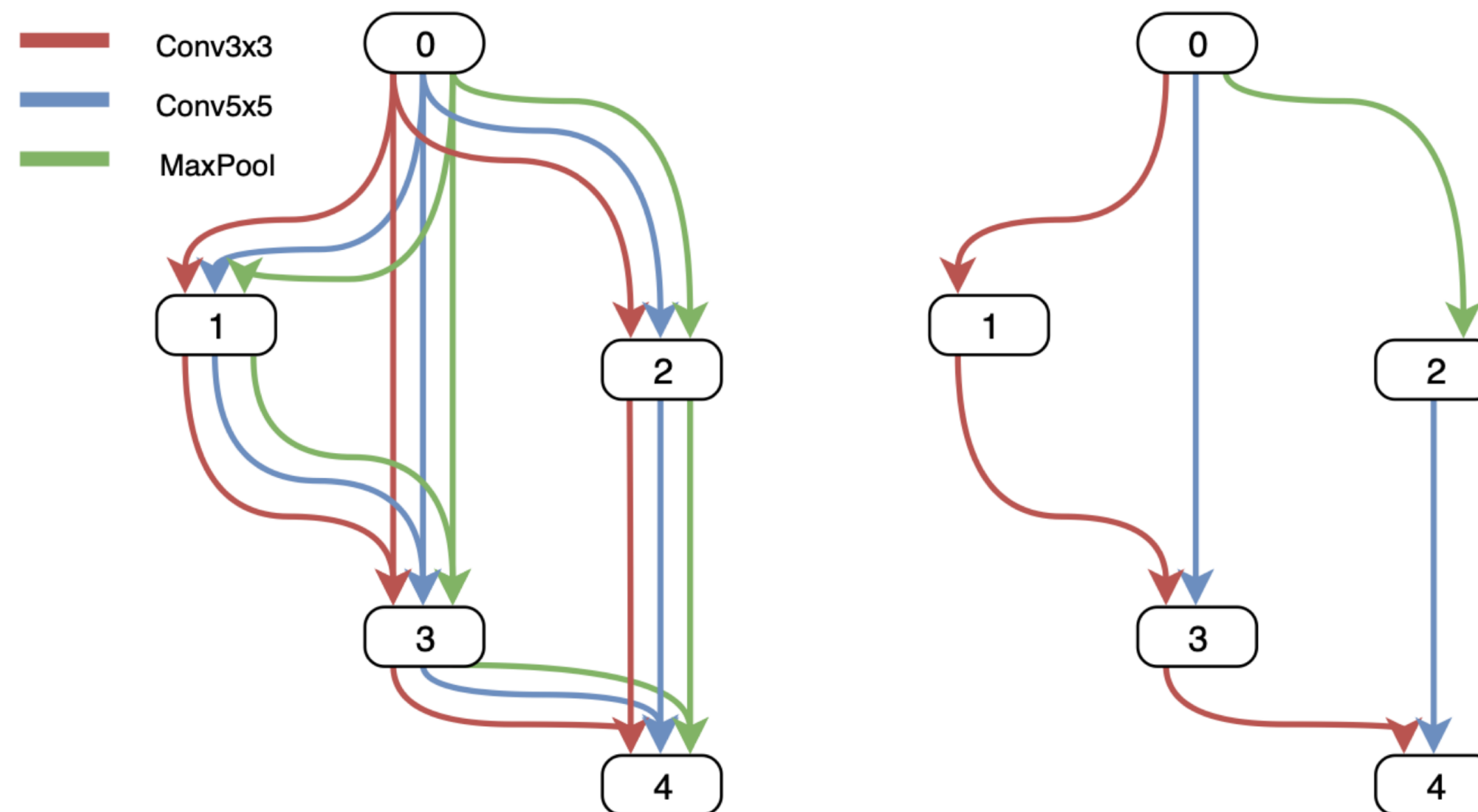
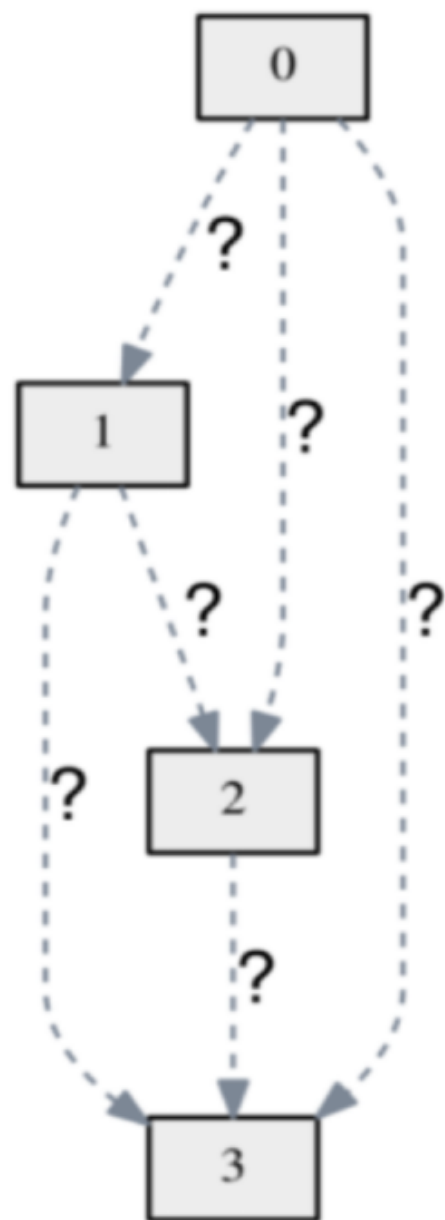


Figure 2. The graph represents the entire search space while the red arrows define a model in the search space, which is decided by a controller. Here, node 1 is the input to the model whereas nodes 3 and 6 are the model's outputs.

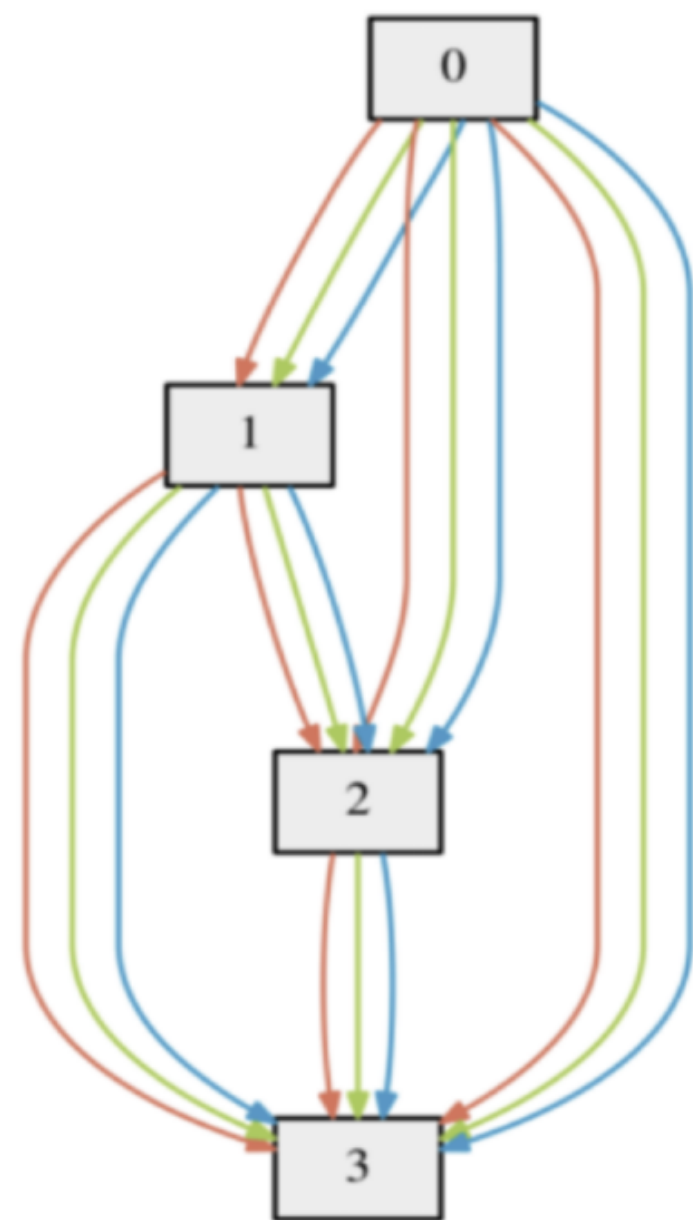
Joint training

- We can use differentiable relaxation for optimizing the connectivity as well
 - Example. DARTS uses GD for finding the subgraph as well
 - Intermediate features are connected with a mixture of modules

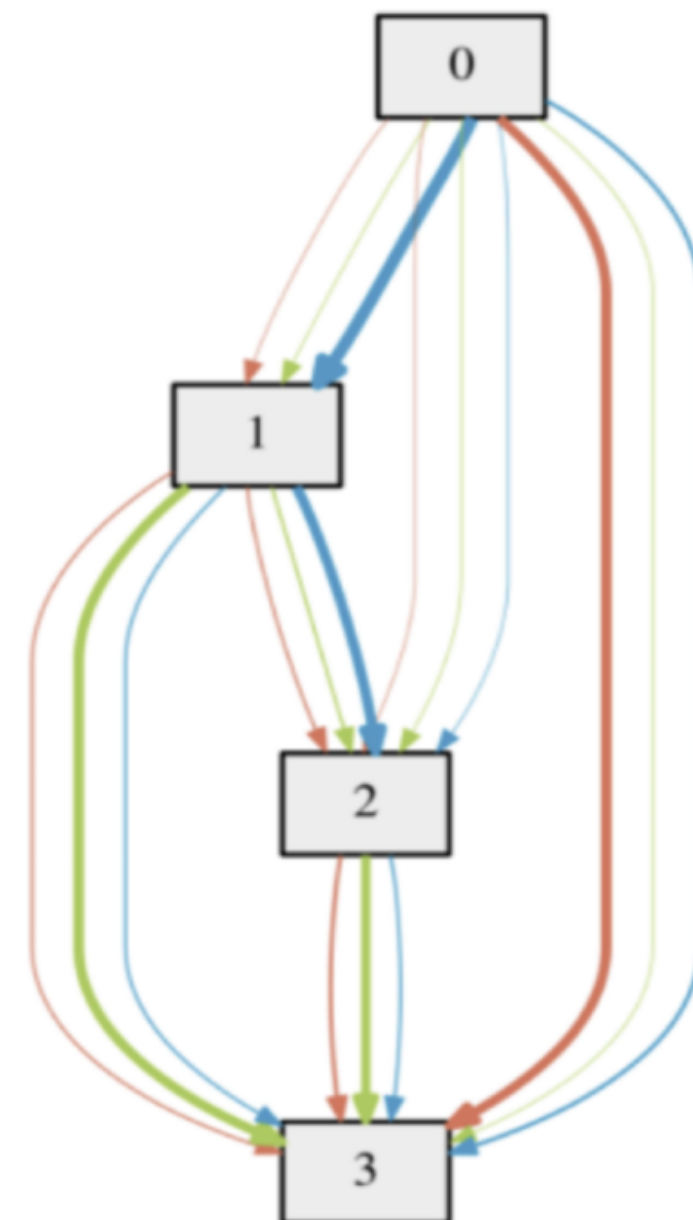




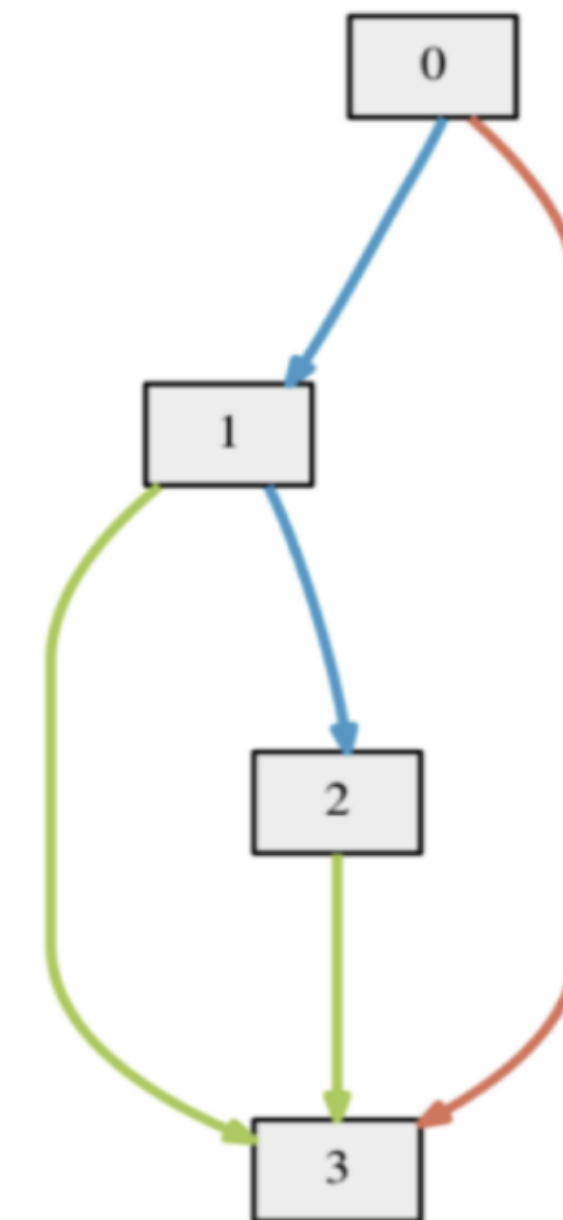
(a) Initially unknown operations on the edges.



(b) Continuous relaxation by placing a mixture of operations on each edge.



(c) Bilevel optimization to jointly train mixing probabilities and weights.



(d) Finalized the model based on the learned mixing probabilities.

$$x^{(j)} = \sum_{i < j} o^{(i,j)}(x^{(i)})$$

$$\bar{o}^{(i,j)}(x) = \sum_{o \in \mathcal{O}} \frac{\exp(\alpha_o^{(i,j)})}{\sum_{o' \in \mathcal{O}} \exp(\alpha_{o'}^{(i,j)})} o(x)$$

Algorithm 1: DARTS – Differentiable Architecture Search

Create a mixed operation $\bar{o}^{(i,j)}$ parametrized by $\alpha^{(i,j)}$ for each edge (i, j)

while not converged do

1. Update architecture α by descending $\nabla_{\alpha} \mathcal{L}_{val}(w - \xi \nabla_w \mathcal{L}_{train}(w, \alpha), \alpha)$
($\xi = 0$ if using first-order approximation)
2. Update weights w by descending $\nabla_w \mathcal{L}_{train}(w, \alpha)$

Derive the final architecture based on the learned α .

Further reading

- Zero-shot NAS
 - Mellor et al., “NAS without training” ICML 2021
 - Abdelfattah et al., “Zero-cost proxies for lightweight NAS” ICLR 2021
- Efficiency-aware NAS
 - ProxylessNAS: Use “latency” as a reward as well
 - MobileNAS: Construct search space with efficient modules
 - MCUNet: Maximize FLOPs for better memory-accuracy tradeoff
 - ChamNet: Train proxies for efficiency metrics

Next Class

- Efficient Training & Tuning

That's it for today 🙌